

Advances in Friction-Induced Vibration in Applied Engineering

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Friction plays a crucial role in various engineering fields, including advanced manufacturing, transportation, aerospace, and bioengineering. It is a fundamental factor that determines the efficiency, reliability, and lifespan of mechanical systems. Friction serves as a primary damping source in dynamic environments, typically stabilizing vibrating systems by consuming system energy. However, friction can also cause counterintuitive self-excited vibration known as friction-induced vibration (FIV). FIV is a significant and challenging vibration problem that exists in various fields. The manifestation of FIV can be flutter or unfavorable noise in most cases [1]. Typical examples are automotive or aircraft brake squeal [2], the unstable vibration of the drill string [3] or cutting machines [4], squeaking human or artificial joints [5], and rattling robot joints [6].

Over the past few decades, scholars have dedicated their efforts to gaining a better understanding of the mechanisms [7,8] and propensity of FIV [9]. It is accepted that the mechanisms basically fall into four categories: (1) the negative gradient in the relations of friction force and velocity (2); stick–slip instability [10,11], which is caused by the difference between static and kinetic friction forces; (3) mode-coupling instability [12] or mode lock-in instability caused by the geometric characteristics of the frictional structure; (4) and sprag-slip instability [13]. Stick–slip mechanisms have a broader range of applications compared with other mechanisms [11,14,15], which is demonstrated below. Investigating the mechanisms underlying FIV remains a highly active and ongoing topic [16,17]. For example, Fang et al. [17] pointed out that the high-frequency vibration of the frictional system could be aroused by the partial separation between the slider and the moving substrate even without mode-coupling instability.

The most well-known FIV issue is commonly referred to as brake squeal. In the automotive industry, over 50% of the research conducted by friction material suppliers is allocated towards understanding and addressing this challenging noise problem [18]. Research on brake noise has been underway for almost a century, preceding research in other fields. Therefore, a significant amount of important research on self-excited vibrations induced by friction has been carried out within the framework of investigating brake noise [19]. The advancements in high-speed transportation have led to increasing concerns regarding railway brakes [20] and wheel/rail noise [21], primarily due to the adverse effects of noise pollution on both the environment and human health [22].

Previous studies have investigated various phenomenological sources that contribute to FIV, including friction laws, geometry, operational conditions (the loading force and the velocity), and surface topography [23,24], leading to different research branches. In recent times, engineering advancements have led to a demand for the detailed modeling of frictional systems. Factors such as uncertainty [25], new materials [26,27], nonlinearities/nonsmoothness [28,29], computational accuracy [30], and efficiency [31] are all areas of concern. Lacerra et al. [32] developed a novel stochastic friction model that incorporates a perturbative term based on Coulomb friction. This modification enables the friction law to replicate the FIV of two rough surfaces without taking into consideration the surface



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topography. In Ref. [33], the irregular vibration of a disc model was compared using various friction laws, and it was discovered that the irregular friction formulation had a more significant effect on the amplitude of instability rather than on the unstable behavior itself. Lazzari et al. [27] investigated the friction behavior and dynamic instability of carbon/carbon composite materials, in which both mode-coupling instability and the negative slope of friction laws were observed. Do et al. [34] proposed a novel strategy for an instability analysis of FIV, which has been shown to maintain accuracy while significantly reducing computational time. Stender et al. [35] proposed a purely data-driven approach for detecting the occurrence of FIV and predicting the onset time of FIV.

Scholars have recently recognized that friction-induced vibration is not solely detrimental to engineering but could also have benefits. In contrast with other methods of converting vibration energy into electrical energy, friction-induced vibration does not depend on ambient vibration sources. New harvesting devices [15,36–39] that utilize FIV based on various energy harvesting technologies, such as electromagnetic, electrostatic, piezoelectric, and triboelectric, have been developed. Fu et al. [15] introduced a triboelectric energy harvester that utilizes a vibro-impact system, which effectively harvests energy from low-frequency ambient vibrations by using the chatter- and stick-slip-induced low-frequency vibrations in the vibro-impact system. Recently, the performance of the harvesters has been improved by combining different technologies. Zhao and Ouyang [39] developed a triboelectric energy harvester with grating-patterned films and magnetic biostability, showing notable improvements in harvesting efficiency.

In addition, FIV in robot finger or arm joints is a significant concern for precise control and positioning. Researchers [40] have utilized stick-slip transitions to drive the locomotion of soft robotics, and the tactile sensing function of robots or mechanical arms relies on vibration signals to identify and monitor object characteristics [41,42]. Investigations into the tactile sensation of texture have been conducted on various surfaces, including textiles [43], and textures with isotropic [42], periodic, or general topographies [44].

At the microscopic level, the emergence of atomic force microscopy and scanning tunnelling microscopy has brought new advances to studying the origin of frictional forces [45–47]. The Prandtl-Tomlinson (P-T) model is the most general model. Following that, extension models based on the P-T model were proposed that can fit the frictional behavior of various materials and incorporate more environmental factors. [48]. Atomic-scale stick-slip friction has been observed on a variety of materials, including metals such as copper and gold [49], sodium chloride [50], and mica [51]. Socoliuc et al. [52] suggested that ultra-low friction can be achieved when stick-slip diminishes. Various velocity-dependent relationships of frictional forces, such as logarithmic velocity dependence, 2/3-order velocity dependence, or square velocity dependence, have been discovered [53,54]. However, the mechanism of multi-atomic stick-slip vibration remains unclear [55,56].

In summary, the multidisciplinary and multiscale effects of friction present challenges in the analysis of friction-induced vibrations. Integrating multidisciplinary technologies can lead to a more comprehensive understanding of the characteristics of frictional forces, providing benefits to multiple engineering fields.

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