



Article Multi-Indicators Decision for Product Design Solutions: A TOPSIS-MOGA Integrated Model

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Abstract: Design decisions occur in all phases of product design and largely affect the merits of the final solution, which will ultimately determine the success or failure of the product in the market. Product design is a continuous process, and a large number of existing studies have proposed decision methods and decision indicators for the characteristics of different stages of design. These methods and indicators can meet the requirements of one of the phases: demand analysis, conceptual design, or detailed design. However, further research can still be conducted on the integration of methods throughout the design phase, using intelligent design methods, and improving the design continuity and efficiency. To address this problem, a TOPSIS-MOGA-based multi-indicators decision model for product design solutions is proposed, including its product design process, decision algorithm, and selection method. First, a TOPSIS-MOGA integrated model for conceptual design and detailed design process is established, the continuity of decision-making methods is achieved by integrating decision indicators. Second, conceptual design solutions are selected through the technique for order of preference by similarity to ideal solution (TOPSIS), based on hesitant fuzzy linguistic term sets and entropy weight method. Finally, detailed design solutions are selected through a multiobjective genetic algorithm (MOGA), based on a polynomial-based response surface model and central combination experimental design method. A case study of the decision-making in the design of high-voltage electric power fittings is presented, the conceptual design phase and the detailed design phase are connected through the indicators, which demonstrates that the proposed approach is helpful in the decision-making of the product design solutions.

Keywords: decision method; multi-indicators; TOPSIS; MOGA; product design

1. Introduction

Studies show that the product design phase accounts for only 12% of the total cost of product development but can affect 75% of the final cost [?]. The design process is a complete process including the requirements analysis stage, conceptual design stage, and detailed design stage [?], in this process, workflow, knowledge flow, and information flow interact with each other, many design solutions are generated at each stage [?]. The product design can be completed only through the complete three stages [?], and the design continuity needs to be noticed [?]. As researchers continue to study the field of product design, intelligent design methods are becoming increasingly important [?]. These methods focus on design process models [?], the product design solution methods [?], and the product design support technologies [?]. These methods will further promote the development of product design, improve the continuity and efficiency of design [?].



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Design solution decision-making is an important factor in product design [?], good or bad design solutions directly affect the effectiveness of the enterprise. Good decisionmaking solutions can not only save a lot of costs and resources but also enhance product competitiveness. How the designer selects the optimal solution from many alternatives, and moves on to the next steps of design or production practice is a key issue in the product development process [?]. What's more, plenty of intelligent methods play a major role in the decision-making process, the collaborative evaluation methods [?], the rough set approach [?], the artificial intelligent evaluation methods [?], the multicriteria decision-making approach [?] and so on, can help to make a better solution.

At present, a large number of scholars have studied the methods of program decisionmaking at different stages, these methods usually have different indicators. Multiple indicators are involved in the conceptual design and detailed design solution decisions, and these indicators sometimes conflict with each other and vary in importance [?]. Design is a continuous process, and the indicators and parameters needed for detailed design need to be considered at the time of conceptual design [?]. In this process of making decisions using different methods and indicators in conceptual design and detailed design, the efficiency of the design is also affected. So, it is necessary to establish a process to integrate decision methods and indicators for conceptual design and detailed design phases.

The study is organized as follows. A review of related studies is presented in Section 2. A framework of the TOPSIS-MOGA-based multi-indicators decision model is presented in Section 3, which demonstrates a typical design process, and introduces different decision methods and indicators of conceptual design and detailed design. Section 4 introduces the model and describes its steps. The TOPSIS-based approach to conceptual design decisions, MOGA-based approach to detailed design decisions and their indicators are also introduced in this section. Section **??** describes the application of the proposed framework and methodology in the design of a high-voltage electric power fitting. The case demonstrates the feasibility of the proposed method, which allows for improved design direction and thus more efficient and continuous design. Finally, the conclusion is presented in Section **??**

2. Related Work

2.1. Product Design Process Study

The product design process is divided into requirements analysis, conceptual design, and detailed design, and the related research includes three main parts: the product design process model, the product design solution method, and the product design support technology.

In the product design process area, Camelo et al. developed an interaction model that extends the search space of design solutions by extending the relationships between levels of abstraction [?]. Li et al. establish a framework approach for user participation in configuration design of complex products to achieve [?]. Zheng et al. proposed a configuration design method for mechatronic systems in the context of industrial manufacturing and constructed a corresponding solution configuration method and process for the detailed design phase [?]. Guo et al. proposed a resilient design methodology and process for the conceptual design phase, using functional decomposition and conflict resolution to support resilient conceptual design [?].

In the product design solution method area, function-behavior-structure (FBS) is a widely used solution model that connects the conceptual design and detailed design phases [?] and expresses the design process by establishing a mapping relationship between function, behavior, and structure. Based on the basic FBS model, FBS-based models such as B-FES [?], FSMEE [?], FPBS [?], and RFBS [?] have been proposed one after another.

Some researchers have built models combining conceptual design with detailed design. Zhao et al. identified a novel approach based on the quantification of Kano's model for integrating requirements into product engineering characteristics [?]. Jiao et al. proposed an approach that used online data to map the requirements into product configurations, including the product transaction data and users' review data [?]. However, they give a serious imbalance to concept design and give more consideration to the configuration design. In our preliminary study, we focused much on discussing a particular phase, the conceptual design phase [?], or the detailed design phase [?], rather than considering both as equally important but separate.

In the product design solution method area, Zhang et al. established a quality-functionknowledge-deployment model, given the different knowledge requirements of the conceptual design stage, structural design stage, detailed design stage, and production planning stage, linking the knowledge requirements of different design stages with product knowledge [?]. To improve the accuracy of knowledge pushing and promote knowledge sharing and reuse, Jiang et al. realized the construction of a knowledge pushing system by machine learning through user data feature extraction, user interest model construction, and recommendation algorithm optimization [?]. These technologies support the design process at the methodological, systemic level.

An effective model can play a good role in promoting the design and improving the efficiency of the design. The applicability of the model depends on the method used. For multistage problems, different methods need to be integrated into a structured process.

2.2. Product Decision Methodology Study

In the decision-making process of design solutions, decision indicators cannot exist outside of the method. The realization of the decision-making method requires the establishment of indicators [?]. At present, a large number of scholars have studied this issue.

In the conceptual design phase, TOPSIS is a widely used method applied to ranking problems [?]. Alternatives are evaluated based on Euclidean distances from an ideal and a nonideal solution [?]. The ideal solution is the solution that satisfies all expectations of the user, which may not exist due to the neglect of various constraints. In addition, many other methods have been applied in the conceptual design phase. Chatterjee et al. integrated the AHP method with the VIKOR method and proposed a flexible multi-indicators decision model, which can solve the problem of inaccurate data and information generated in expert judgment decisions [?]. Chunhua F et al. proposed functional, manufacturing, economic, environmental, recyclable, and social properties as evaluation indicators for group decision-making based on intuitive fuzzy preferences in the conceptual design phase for sustainable design [?]. Guo et al. select the optimal solution by matrix deployment, candidate solution generation, and interactive genetic algorithm solution for the low carbon indicator in the conceptual design [?]. He et al. proposed a functional model and a corresponding physical parameter model and established a comprehensive model of functional and solution libraries based on the spatial matrix to realize the decision-making of design solutions [?].

In the detailed design phase, Song K et al. proposed a combination of computational fluid dynamics analysis and various experimental design methods for multiobjective decision-making, using artificial neural networks for six design variables at the rear of the Ahmed body for the problem of reducing drag and lift coefficients of the vehicle [?]. Feng et al. proposed a digital twin approach to decision-making for product design solutions. It is capable of physical data and emotional feedback [?]. Yi et al. proposed a VIKOR-based decision method for reconfigurable machine tool design solutions, defined the modular similarity between reconfigurable and prototype machine tools, and established three quantitative evaluation indicators: modular chain similarity, modular interface complexity, and reconfiguration cost [?]. Yang et al. proposed a mechatronic model based on motion characteristics and error sources for the solution decision of a direct-drive feed system, based on noise, disturbance, mechanical vibration, and other indicators [?].

Currently, these decision methods and indicators can only be used in one design phase, and the methods and indicators in the conceptual and detailed design phases are separated, which reduces the continuity of the design process.

2.3. A Brief Summary

Although the product design process models, solution methods, support technologies, and decision methods have advanced recently, it is still challenging to improve the efficiency of product design. Several factors have hindered its development and adoption:

- (1) In the product design process, there is a lack of a structured model linking conceptual and detailed design, and the related solution methods and supporting technologies are usually only adapted to a specific stage.
- (2) There is no continuity between decision methods at different stages, and the same product will use completely different indicators and methods at different design stages, which leads to the compromised direction in decision-making.

Although several previous studies have investigated the impact of different design process models and decision methods on product design, it is still a challenge to connect the processes, methods, and indicators of conceptual and detailed design. Thus, a holistic process that addresses both conceptual and detailed design characteristics, with supporting decision methods is needed to solve these challenges.

3. Multi-Indicators Decision Model for Product Design Solutions Based on TOPSIS-MOGA

The multi-indicators decision model based on TOPSIS-MOGA is shown in Figure 1. The multi-indicators decision model of product design solution can be divided into three layers: the design process layer, the indicator layer, and the decision method layer. The design process layer is a design process based on the serial design model, which divides the product design into three stages: requirement analysis, conceptual design, and detailed design, which can guide designers to carry out product design in a clear and organized manner, ensure the quality of product design and reduce design costs; the indicator layer, based on the characteristics of the design process, divides the relevant indicators into functional-structural indicators and performance indicators to form The decision method layer provides the decision method of requirement analysis, conceptual design, functional design plan, structural design plan and detailed design plan in the product design process, which can help designers to make decision activities of design plan scientifically, to improve the design efficiency and shorten the product development cycle.

In the full cycle of product design, the relevant indicators have been changing, from those that focus more on time, quality, cost, resources, and environment in conceptual design to those that pay more attention to structural strength, spacing, and fatigue limits in detailed design, which are different but still have continuity. In the conceptual design stage, a TOPSIS-based product solution decision method is constructed to assist designers in solution decision-making, through evaluation statement identification based on hesitant fuzzy linguistic term sets, evaluation matrix construction based on TOPSIS, and decision calculation based on entropy weight method. Hesitant fuzzy linguistic term sets are used when experts hesitate to choose appropriate linguistic terms to assess a linguistic variable. In the detailed design stage, the MOGA-based solution decision method is established, the solution performance indicators are constructed, the detailed design solution set is constructed through the combination of discrete parameters and their boundary conditions, and the decision calculation is carried out based on MOGA to realize the solution decision.



Figure 1. The framework of the multi-indicators decision model.

4. Methodology

4.1. Product Design Solutions with Multi-Indicators

In the decision-making process of design solutions, indicators play an important role to meet the needs of users, and as the design process continues, these indicators also change, such as technical performance [?], energy consumption [?], complexity [?], etc., these indicators will be able to provide a reference for program decisions. This paper summarizes the comprehensive evaluation indicators of the product design, as shown in Figure 2.

- (1) Technical performance, including the degree of standardization of components [?], the process performance, the functional parameters, and the structural rationality [?], etc.;
- (2) Economy, including the material cost, the manufacturing cost, the installation cost, the maintenance cost, and the production cycle [?], etc.;
- (3) Human-machine performance, which includes safety, aesthetic comfort, usability [?], maintainability [?], etc., and may involve human participation in the whole life cycle of the product, including transportation, installation, operation, and maintenance;
- (4) Social performance, including sustainability [?], environmental protection and energy conservation [?], etc.;
- (5) Innovation, including the technological innovation [?], the application innovation and the form innovation [?], etc.;

When conceptual design and detailed design are carried out, the corresponding decision methods are different and their indicators are different, but they still have a strong connection. The indicators used in the conceptual design stage are called functional-structural indicators, and the indicators in the detailed design stage are called performance indicators, and the performance indicators are further refinements of the functional-structural indicators, and the decision indicators in each stage cascade from general to specific, in line with the product design process characteristics of the product design process.





4.2. TOPSIS-Based Decision Method for Product Conceptual Design Solutions

TOPSIS is a common decision-making method that ranks alternatives according to the degree of approximation to the ideal solution [?]. Due to the high degree of uncertainty and ambiguity of the solutions in the conceptual design stage, the TOPSIS method cannot be fully adapted, so hesitant fuzzy linguistic term sets, entropy weight method, and TOPSIS method are integrated to form a TOPSIS-based decision-making method. The method is divided into three parts, evaluation statement identification based on hesitant fuzzy linguistic term set, evaluation matrix construction based on TOPSIS, and decision calculation based on entropy weight method, as shown in Figure 3.

4.2.1. Evaluation of Statement Recognition based on Hesitant Fuzzy Linguistic Term Sets

Hesitant fuzzy linguistic term set can represent the assessments when decision-makers hesitate about several fuzzy linguistic terms, in which the "min_upper" and "max_lower" operators are provided to carry out hesitant fuzzy linguistic decision-making problems [?]. The core idea of hesitant fuzzy linguistic term set theory is to transform the context-independent grammatical evaluation language given by the evaluator into a hesitant fuzzy linguistic term set through a conversion function, and then perform quantitative computation and decision-making based on the hesitant fuzzy linguistic term set [?].



Figure 3. TOPSIS-based product conceptual design solution decision flow chart.

Let the set of linguistic terms $S = \{s_k | k = -\tau, ..., -1, 0, 1, ..., \tau\}$, and if H_S is a set consisting of linguistic terms with continuous subscripts and finite number in S, then H_S is said to be a hesitant fuzzy linguistic term set in the linguistic term set S with

Upper bound :
$$H_{S^+} = max(s_i) = s_i, s_i \in H_S$$
 and $\forall i, s_i \leq s_j$.

Lower bound : $H_{S^-} = min(s_i) = s_i, s_i \in H_S$ and $\forall i, s_j \leq s_i$,

To calculate the distance between two hesitant fuzzy linguistic term sets, let $env(H_S^1) = [s_p, s_q]$ and $env(H_S^2) = [s_{p'}, s_{q'}]$, the distance of H_S^1 and H_S^2 can be calculated as follows [?]:

$$d(H_S^1, H_S^2) = |q' - q| + |p' - p|$$
(1)

The evaluation of alternatives using the hesitant fuzzy linguistic term set requires a context-independent grammar. Let $S = \{s_k | k = -\tau, ..., -1, 0, 1, ..., \tau\}$ be the set of linguistic terms, then its context-independent grammar is

$$G_H = (V_N, V_T, I, P) \tag{2}$$

where, $V_N = \{\text{primary term, compound term, monadic relation, binary relation, conjunction}\}$. $V_T = \{\text{below, greater than, between..., and, } s_{-\tau}, \dots, s_{-1}, s_0, s_1, \dots, s_{\tau}\}; I \in V_N$, is the first term of V_N , and P is the rule.

4.2.2. Construction of TOPSIS-Based Evaluation Matrix

When making decisions, a multi-indicators decision environment needs to be constructed first: the set of alternative conceptual design options A, the set of alternative evaluation indicators C, the set of evaluation experts U and the set of evaluation language terms *S* need to be built. It is assumed that the evaluation language term set contains seven language terms:

 $S = \{s_{-3}: Worst, s_{-2}: Very poor, s_{-1}: Poor, \}$

 s_0 : Medium, s_1 : Good, s_2 : Very good, s_3 : Best}

The corresponding context-independent language evaluation matrix can be constructed based on Equation (2), as shown in Table **??**.

Table 1. Context-independent language evaluation matrix $D^1(ll_{ij})$.

	<i>C</i> ₁	 C_n
A_1	Poor	 Lower than very poor
÷	:	 ÷
A_m	Between good and poor	 Higher than very good

The hesitant fuzzy linguistic term set decision can be constructed based on Equation (1), as shown in Table **??**.

	<i>C</i> ₁		C_n
A_1	$\{s_{-1}\}$		$\{s_{-3}, s_{-2}\}$
:	:		:
A_m	$\{s_{-1}, s_0, s_1\}$	•••	$\{s_2, s_3\}$

Table 2. Hesitant fuzzy linguistic term set decision matrix $\widetilde{X}^3(H^3_{S_{ii}})$.

Where $H_{S_{ij}}^{\alpha} = \left\{ s_{\delta_l^{\alpha i j}} \middle| s_{\delta_l^{\alpha i j}} \in S, l = 1, 2, ..., L \right\}, \delta_l^{\alpha i j}$ denotes the subscript of the linguistic terms and *L* is the length of the set of hesitant fuzzy linguistic terms.

(3) Decision-making calculation based on the entropy weight method

In order to reduce the subjective factors in the program evaluation process, the entropy method index is used to assign weights, which can effectively reduce the interference of human factors to obtain accurate decision results [?].

For the hesitant fuzzy linguistic term set H_S , its entropy can be expressed as

$$E(H_S) = 1 - \frac{2}{L} \sum_{l=1}^{L} \frac{|\delta_l|}{2\tau}$$
(3)

where δ_l is the subscript of linguistic terms in H_S and $L = l(H_{S_{ij}})$ is the length of the set $H_{S_{ii}}$ of hesitant fuzzy linguistic terms, the number of linguistic terms in H_S .

Therefore, for the set of equipment selection design solutions $A = \{A_i | i = 1, 2, ..., m\}$, the set of evaluation indicators for the solution is $C = \{C_j | j = 1, 2, ..., n\}$, the set of linguistic terms for program evaluation $S = \{s_k | k = -\tau, ..., -1, 0, 1, ..., \tau\}$, and the average entropy of the evaluation index is:

$$E_{j} = \frac{1}{k} \frac{1}{m} \sum_{\alpha=1}^{k} \sum_{i=1}^{m} E(H_{S_{ij}}^{\alpha})$$
(4)

The weights are:

$$\omega_j = \frac{1 - E_j}{n - \sum_{j=1}^n E_j} \tag{5}$$

After the weights are calculated, the evaluation indicators are divided into efficiency indicators (the larger the indicator the better) and cost-based indicators (the smaller the

$$\widetilde{V}_{j}^{+} = \left[\left(\left(\begin{pmatrix} \alpha = 1 \\ max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} max \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \end{pmatrix} | j \in \Omega_{b}, \begin{pmatrix} \alpha = 1 \\ min \begin{pmatrix} i = 1 \\ min \begin{pmatrix} max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} k \\ max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \end{pmatrix} | j \in \Omega_{b}, \begin{pmatrix} \alpha = 1 \\ min \begin{pmatrix} i = 1 \\ min \begin{pmatrix} max \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \end{pmatrix} | j \in \Omega_{c} \end{pmatrix} \right]$$

$$\widetilde{V}_{j}^{-} = \left[\left(\left(\begin{pmatrix} \alpha = 1 \\ min \begin{pmatrix} i = 1 \\ min \begin{pmatrix} min \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \right) \right) | j \in \Omega_{b}, \begin{pmatrix} \alpha = 1 \\ max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} max \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \end{pmatrix} | j \in \Omega_{c} \right)$$

$$\left(\left(\begin{pmatrix} \alpha = 1 \\ min \begin{pmatrix} i = 1 \\ min \begin{pmatrix} k \\ min \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \right) | j \in \Omega_{b}, \begin{pmatrix} \alpha = 1 \\ max \begin{pmatrix} i = 1 \\ max \begin{pmatrix} max \begin{pmatrix} k \\ S_{ij} \end{pmatrix} \end{pmatrix} \end{pmatrix} | j \in \Omega_{c} \right) \right]$$

$$(7)$$

They are recorded as

$$\widetilde{A}^{+} = \left(\widetilde{V}_{1}^{+}, \widetilde{V}_{2}^{+}, \dots, \widetilde{V}_{n}^{+}\right)$$

$$\widetilde{A}^{-} = \left(\widetilde{V}_{1}^{-}, \widetilde{V}_{2}^{-}, \dots, \widetilde{V}_{n}^{-}\right)$$
(8)

The weighted distance of the design solution to the positive and negative ideal solution are calculated, and can be expressed as follows:

$$D_i^+ = \sum_{j=1}^n \frac{1}{\omega_j} d\left(x_{ij}, \widetilde{V}_j^+\right)$$

$$D_i^- = \sum_{j=1}^n \omega_j d\left(x_{ij}, \widetilde{V}_j^-\right)$$
(9)

where $d(x_{ij}, \tilde{V}_j^+)$ and $d(x_{ij}, \tilde{V}_j^-)$ are calculated by Equation (1).

Finally, the posting schedule of the program can be expressed as follows:

$$RC(A_i) = \frac{D_i^-}{D_i^+ + D_i^-}, i = 1, 2, \dots, m$$
(10)

The greater the relative closeness means the closer the design solution is to the positive ideal solution, the better the design solution is. MATLAB 6.0 is used to finish the calculation of decision-making. At this point, the solution decision process of conceptual design is completed.

4.3. MOGA Algorithm-Based Decision Method for Detailed Product Design Solutions

The detailed design phase of the product mainly focuses on the dimension of components, combining multiple dimensions to obtain the optimal design solution, and finally outputting the detailed assembly drawings and component engineering drawings of the product. In this stage, the formed solutions appear in parametric form, and the number of these combined solutions is huge, and it is difficult to determine the optimal design solution by the decision maker's preference information. In this paper, we propose a MOGA algorithm-based decision-making method for product detailed design solutions, constructing decision indicators for product detailed design solutions, constructing a sample set of detailed design solutions based on the central combination test method, and MOGA multiobjective optimization to achieve solution decision-making. The flow chart is shown in Figure **?**?.



Figure 4. MOGA-based product detail design solution decision flow chart.

4.3.1. Construction of Decision Indicators and Decision Target

Based on functional-structural indicators, the indicators will be further evolved and refined. As the detailed design stage is mainly designed for dimensional parameters, further indicators are determined, such as structural strength, safety factor, inherent frequency, structural quality and a series of other factors that needs to be considered when making decisions.

The multi-indicator decision-making for detailed product design mainly consists of the following three elements: (1) objective function, that is, the requirements that the decision problem wants to achieve, is a function of the composition of the decision variables, such as the objective function is the structural strength (noted as *SS*), the safety factor (noted as *SF*), the inherent frequency (noted as *NF*) and the structural quality (noted as *SM*); (2) decision variables—the decision variables in the detailed design program decision are generally the dimensional parameters of various components, which have a large impact on the objective function; (3) constraints—the decision variables are limited by the resources, generally expressed as a range of values. They are noted as follows:

$$max(min)F(X) = [f_1(x), \dots, f_m(x)]$$
s.t.
$$\begin{cases}
g_r(x) \le 0, r = 1, 2, \dots, R \\
h_k(x) = 0, k = 1, 2, \dots, K \\
x_i^L \le x_i \le x_i^U, i = 1, 2, \dots, n
\end{cases}$$
(11)

where *X* denotes the set of alternative design solutions, and the number of alternative design solutions in the detailed design solution decision problem is generally large or

infinite, x_i is the decision variable, f_m is the objective function, $g_r(x)$ is the inequality constraint, and $h_k(x)$ is the constraint.

4.3.2. Construction and Consistency Test of Detailed Design Solution Sample Set

After determining the objective function, decision variables, and constraints according to the evaluation index of the detailed design, in order to conduct a multi-indicators optimization search and finally determine the optimal detailed design, it is necessary to build a sample set of design solutions consisting of decision variables and establish the functional relationship between the objective function and the decision variables. In this paper, the central combination experimental design method is chosen to generate the sample set of detailed design solutions. After obtaining the sample points of the decision variables by the central combination experimental design method, it is necessary to obtain the values of the objective function concerning each sample point. To shorten the product development cycle and reduce the development cost, this method uses 3D modeling software and finite element analysis method to obtain the value of the objective function of each sample point. The 3D modeling software establishes a 3D model of the detailed design solution, composed of the dimensions of the decision variables determined by the central combination test method, and then imports the 3D model into the finite element analysis software ANSYS Workbench 12.0, and the sample set can be determined according to the constraints of the decision variables using the central combination test method in the design exploration optimization module.

With the sample set constructed, a polynomial-based response surface model is also needed instead of the objective function to achieve fast computation. The response surface model can be expressed as follows:

$$\widetilde{y}(x) = a_0 + \sum_{i=1}^n b_i x_i + \sum_{i=1}^n b_{ii} x_i^2 + \sum_{i=2}^n \sum_{j=1}^{i-1} b_{ij} x_i x_j$$
(12)

where a_0 is a constant, b_i , b_{ii} and b_{ij} are the primary, square and mixed term coefficients, respectively, and n is the number of variables.

The consistency test is performed using the decidable coefficient R^2 , the adjusted decidable coefficient Ra^2 , and the root mean square error σ_{RMSE} .

$$R^{2} = \frac{\sum_{i=1}^{p} (\tilde{y}_{i} - \bar{y})^{2}}{\sum_{i=1}^{p} (Y - \bar{y})^{2}}$$

$$R_{a}^{2} = 1 - \frac{\sum_{i=1}^{p} (\hat{y}_{i} - \bar{y})^{2} (p - 1)}{\sum_{i=1}^{p} (Y - \bar{y})^{2} (p - k - 1)}$$

$$\sigma_{RMSE} = \sqrt{\frac{1}{p} \sum_{i=1}^{p} (Y_{i} - \tilde{y}_{i})^{2}}$$
(13)

where \tilde{y}_i is the predicted value of the response surface model, Y is the actual observed value of the system output, \bar{y} is the mean of the actual observed value, p is the number of test points, and k is the statistical degrees of freedom. The values of the determinable coefficient and the adjusted determinable coefficient are in the range of [0,1], which describe the degree of explanation of the design variables to the target function. The closer the value is to 1, the better the explanation of the target function by the response surface model. The root means square error describes the distance between the predicted value of the response surface model and the actual observed value of the target function, and the closer the value is to 0, the better the accuracy of the fit of the response surface model.

4.3.3. Optimization of Multiobjective Genetic Algorithm

Traditional multiobjective optimization uses the weighting method, the constraint method and the utility function to convert multiobjective optimization problems into single-objective optimization problems, which is simple and fast convergence, but often has only

one optimal solution, which is difficult to meet the requirements of designers in the detailed design program decision problem. MOGA is a multiobjective optimization algorithm based on a genetic algorithm, which can obtain a set of optimal solutions in one run, is easy to implement without gradient information [?], and can meet the requirements of design solution decision in the detailed design phase. The process of MOGA includes seven steps:

- Generate the initial population: randomly generate the initial population with a certain number of individuals and genetically code the population individuals using Gray's coding, in order to reduce the number of operations while ensuring the population diversity to avoid premature convergence;
- (2) Determine the fitness function: determine the fitness function according to the actual objective function, taking into account both the ranking level of the population individuals and the average fitness value;
- (3) Selection operation: according to the fitness value of individuals, the selection operator determines which individuals are retained into the next generation population and which individuals are eliminated;
- (4) Crossover operation: parental chromosomes are crossed over to produce a new generation of genetic individuals to ensure the diversity of the population;
- (5) Mutation operation: the mutation operator causes the parental chromosome code to change, increasing the diversity of the population, and the mutation can avoid the population from producing premature maturity problems;
- (6) Pareto solution set generation: the optimal solution set satisfying the objective function, generated by the elite retention strategy;
- (7) Termination condition: the condition for evolution to stop, usually determined by the number of generations of the artificially set iterations. After the termination of the iteration, the designer selects a satisfactory solution from the Preto solution set and ends the solution decision process of detailed product design.

The MOGA can be calculated by MATLAB 6.0, the maximum number of iterations of MOGA, the initial population, the crossover rate, and the variable rate needs to be set.

5. Case Study

5.1. Introduction

A split drape coupling plates are a kind of electric power fitting, mainly used in extra-/ultrahigh voltage transmission lines and they play a role in transmitting the mechanical load of transmission lines. A schematic diagram is shown in Figure ??. The position of the coupling plate in different structures is different, but that is to bear the load and keep the wire position. In the ultrahigh voltage transmission lines, due to the number of wire splits—the characteristics of large wire tension—the split drape coupling plate needs to bear great loads. On failure, it will trigger the whole drape string of accidents, will impact on the stable operation of the power grid, industrial and agricultural safety production.

With the transmission voltage getting higher, the split drape coupling plate must have higher load capacity, higher anticorona capability, and a more innovative structure. With the transmission distance getting longer, the split drape coupling plate must get lighter with a higher antibumping capacity. It must also meet increased demands for lower cost, longer service life, easy installation and maintenance. The cross-sectional area of the conductor is getting larger, which has higher requirements on more splits, easier production, safer and more reliability. All the mechanical performance, electrical performance, and environmental protection of the supporting products to be better noticed.



Figure 5. Schematic diagram of split drape coupling plates on a transmission line.

5.2. Conceptual Design and Solution Decision

Using the affinity diagram method to analyze the customer needs of the product and summarizing and organizing the five aspects of technical performance, economy, manmachine, social, and innovation, a quality house can be constructed as shown in Figure **??** (removing the right wall).

Related symbol

Strongly positive correlation									
Strongly negative correlation									
+ Positive correlation									
- Negative correlation									
Technic	cal				A	Ľ			
characteri	stics	Stru	Met	Pa	nti-s	oad o	Relia	a	We
Customer		ctur	erial	urts	ickn	apa	abili	ost	ight
needs and		e	s		ess	city	ţ		
Six Splits	5	9							
Light weight	4	1	3	1				1	9
Anti humping	2	1	5	1			1	1	
Anti-bumping	3	9	2	1			1		
High load capacity	4	9	3			9	1		
Long service life	2	3			3	1	3	1	
Easy production	2	3	1	9				5	
Low cost	1	1	5	3				9	3
Safe and reliable	3	3	1		3	3	9		
Easy installation	1	3		5					5
Easy maintenance 2		3		1					
Anti-corona		1	3	3	9		1		
Novel structure 1									
Importance of technical			4	4	3	4	4	2	4
features			0	1	3	7	2	5	4
Importance Rankin	g	1	6	5	7	2	4	8	3

Figure 6. Split drape coupling plate design quality house (part).

It can be seen that the structural layout has the greatest influence on the design of the whole split drape coupling plate from Figure ??, which is the most important technical feature. Therefore, the design of the structural layout is mainly considered in the functional design phase of the conceptual design. According to the correlation matrix of technical features, it can be seen that there are negative correlations between technical features, i.e., conflicts arise. The negative correlations are load-bearing capacity and structural weight, structural weight and reliability, and anticorona capacity and cost. Through the TRIZ theory conflict principle of contradiction and multiple conceptual design solutions can be obtained, as shown in Figure ??.



Figure 7. Conceptual design functional solutions. (a) Conceptual design solution 1. (b) Conceptual design solution 2. (c) Conceptual design solution 3. (d) Conceptual design solution 4. (e) Conceptual design solution 5.

The five conceptual design function solution is based on the "split" invention principle, which divides the original integral traditional split drape coupling plate into two main parts: the small link plate group part, i.e., the black part of Figure **??**, of which each small link plate completes the function of connecting with other electrical fixtures; the mainframe part, i.e., the part indicated by the lines in Figure **??**, so that the small coupling board can keep fixed and complete the layout requirements of six splits.

On this basis, the decision of the product conceptual design plan is carried out, firstly, the technical performance, economic performance, human-machine performance, social performance and innovation are recorded as C_j , j = 1, 2, 3, 4, 5. Based on this, three industry experts were invited as u_1 , u_2 , u_3 , based on language term sets $S = \{s_{-3}: Worst, s_{-2}: Very poor, <math>s_{-1}: Poor, s_0: Medium, s_1: Good, s_2: Very good, s_3: Best\}$. Context-independent language was used to analyze and evaluate the five conceptual design functional solutions, and the context-independent language evaluation matrix was obtained, and the hesitant fuzzy linguistic term set decision matrix was established. Some results are shown in ????

	<i>C</i> ₁	<i>C</i> ₂	<i>C</i> ₃	C_4	<i>C</i> ₅
A_1	Good	Higher than very good	Higher than very good	Between medium and very good	Between good and very good
A_2	Higher than very good	Higher than very good	Very Good	Between good and very good	Higher than good
A_3	Between poor and medium	Medium	Between poor and medium	Between medium and good	Between good and very good
A_4	Between medium and good	Higher than very good	Between good and very good	Between medium and very good	Between medium and good
A_5	Lower than very poor	Between poor and medium	Between poor and medium	Between good and very good	Lower than poor

Table 3. Context-independent language evaluation matrix $D^1(ll_{ij})$.

Table 4. Hesitant fuzzy linguistic term set decision matrix $\widetilde{X}^3(H^3_{S_{ii}})$.

	<i>C</i> ₁	<i>C</i> ₂	<i>C</i> ₃	C_4	C_5
A_1	$\{s_1, s_2\}$	$\{s_1, s_2, s_3\}$	$\{s_2, s_3\}$	$\{s_1, s_2\}$	$\{s_2\}$
A_2	$\{s_2, s_3\}$	$\{s_1, s_2\}$	$\{s_2, s_3\}$	$\{s_1, s_2\}$	$\{s_0, s_1\}$
A_3	$\{s_{-3}, s_{-2}\}$	$\{s_{-3}, s_{-2}, s_{-1}\}$	$\{s_{-3}, s_{-2}\}$	$\{s_0, s_1, s_2\}$	$\{s_1, s_2\}$
A_4	$\{s_1, s_2\}$	$\{s_2, s_3\}$	$\{s_0\}$	$\{s_2, s_3\}$	$\{s_0, s_1\}$
A_5	$\{s_{-3}, s_{-2}\}$	$\{s_{-1}, s_0\}$	$\{s_0, s_1\}$	$\{s_0, s_1, s_2\}$	$\{s_0\}$

Based on the evaluation information given by the decision matrix of the three hesitant fuzzy linguistic term sets, the relative weights of each evaluation index are calculated. The average entropy of each evaluation index is calculated based on Equation (4).

$$E_1 = \frac{2}{5}, E_2 = \frac{41}{90}, E_3 = \frac{22}{45}, E_4 = \frac{31}{54}, E_5 = \frac{17}{30}$$

The entropy weights of each evaluation index are calculated according to Equation (5).

$$\omega_1 = 0.239, \ \omega_2 = 0.217, \ \omega_3 = 0.203, \ \omega_4 = 0.169, \ \omega_5 = 0.172$$

The five evaluation indicators are all benefit indicators, and the positive ideal solution \tilde{A}^+ and the negative ideal solution \tilde{A}^- of the functional solution of the split drape coupling plate conceptual design are obtained according to Equations (13)–(15).

$$\widetilde{A}^{+} = [\{s_3, s_3\}, \{s_2, s_3\}, \{s_2, s_3\}, \{s_2, s_3\}, \{s_2, s_3\}]$$
$$\widetilde{A}^{-} = [\{s_{-3}, s_{-2}\}, \{s_{-3}, s_{-2}\}, \{s_{-3}, s_{-2}\}, \{s_{-1}, s_1\}, \{s_{-3}, s_{-1}\}]$$

The weighted distance from each alternative conceptual design functional solution to the positive and negative ideal solutions can be calculated by MATLAB 6.0 according to Equations (6)–(8).

$$D_1^+ = 2.272, D_2^+ = 1.172, D_3^+ = 6.314, D_4^+ = 2.4, D_5^+ = 5.985$$

 $D_1^- = 6.95, D_2^- = 8.05, D_3^- = 2.908, D_4^- = 6.822, D_5^- = 2.998$

In order to rank the advantages and disadvantages of the five alternative conceptual design function options, the relative closeness of each option is calculated according to Equations (9) and (10), and the higher the value of the relative closeness means that the option meets the design requirements with higher design potential, and the results are calculated by MATLAB 6.0, and is shown as follows:

$$RC(A_1) = 0.754, RC(A_2) = 0.873, RC(A_3) = 0.315, RC(A_4) = 0.74, RC(A_5) = 0.334$$

The second split drape coupling plate conceptual design functional solution (Figure ??b) is the optimal design solution among the five design solutions, which is selected as the final conceptual design functional solution and the decision process is completed.

5.3. Performance Indicators Construction and Detailed Solution Decisions

The detailed design stage of the split drape coupling plate is mainly based on the conceptual design structural solution. The length of each equilateral angle, the size of each connection hole, etc. are determined according to the requirements of the splitting spacing in the design task. According to the technical characteristics in the quality house, the split drape coupling plate has to have higher requirements for load-bearing capacity, reliability as well as quality. The split drape coupling plate is required to have a higher safety factor and smaller quality under the mechanical damage load of 144KN. Therefore, according to the integrated process from function-structure indicators to performance indicators, the detailed design stage of split drape coupling plate mainly focuses on two indicators: safety factor and structural quality.

We focus on the dimensional parameters that have the greatest influence on the functional parameters of the split drape coupling plate. Analysis of the structural design solution of the split drape coupling plate can obtain three factors that have a greater influence on the safety factor and structural quality: the distance of the center hole of the top coupling plate from the edge distance of the coupling plate (noted as x_1 in Figure ??), the thickness of each small coupling plate (noted as x_2 in Figure ??) and the thickness of the equilateral angle (noted as x_3 in Figure ??)



Figure 8. Important dimensional parameters of split drape coupling plate. (**a**) Top coupling plate hole distance and small coupling plate thickness. (**b**) Equilateral angle thickness.

Therefore, x_1 , x_2 and x_3 are used as decision variables in the multi-indicators decision model of split drape coupling plate, and the safety factor (denoted as *SF*) and structural mass (denoted as *SM*) are used as objective functions, while the constraints are determined according to the design task statement and design experience. The multi-indicators decision model for the detailed design solution of split drape coupling plate is established according to Equation (11).

$$\max SF = sf(x_1, x_2, x_3) \min SM = sm(x_1, x_2, x_3) s.t. 25 \le x_1 \le 45 15 \le x_2 \le 30 3 \le x_3 \le 6 \min(SF) \ge 1.5 \\ max(SM) \le 150$$
 (14)

The three-dimensional model of the split drape coupling plate was then established, imported into the finite element analysis software ANSYS Workbench 12.0, and the three-factor, five-level test table shown in Table **??** was determined according to the constraints of the decision variables using the central combination test method in the Design Exploration optimization module.

	** * 1 1	Coding and Levels							
Factor	Variable	-1	$-\alpha$	0	α	1			
Top coupling plate hole distance	<i>x</i> ₁	25	30	35	40	45			
Thickness of small coupling plate	<i>x</i> ₂	15	18.75	22.5	26.25	30			
Thickness of the equilateral angle	<i>x</i> ₃	3	3.75	4.5	5.25	6			

Table 5. Design factor coding and levels.

Twenty-nine detailed design solutions of split drape coupling plate were obtained as the sample set using the central combined test method, and the mechanical analysis of the sample set of design solutions under 144KN load was performed using ANSYS Workbench 12.0 to obtain the safety factor as well as the structural mass output. The test sample set and finite element output results are shown in Table **??**.

Table 6. Experimental data and finite element analysis output.

NT		Input		Ou	tput	NT		Input		Output	
No	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> ₃	SF	SM	No. –	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> ₃	SF	SM
1	25	22.5	4.5	1.516	128.499	16	35	22.5	3	1.115	106.855
2	25	15	3	1.072	86.375	17	35	22.5	3.75	1.347	117.765
3	25	30	3	1.113	127.334	18	35	22.5	6	1.759	149.435
4	25	15	6	1.229	128.955	19	35	22.5	5.25	1.674	139.056
5	25	30	6	1.919	169.915	20	40	22.5	4.5	1.513	128.499
6	30	22.5	4.5	1.515	128.499	21	40	18.75	3.75	1.307	107.526
7	30	18.75	3.75	1.317	107.526	22	40	26.25	3.75	1.279	128.005
8	30	26.25	3.75	1.279	128.005	23	40	18.75	5.25	1.551	128.816
9	30	18.75	5.25	1.488	128.816	24	40	26.25	5.25	1.694	149.296
10	30	26.25	5.25	1.699	149.296	25	45	30	3	1.114	127.334
11	35	22.5	4.5	1.515	128.499	26	45	22.5	4.5	1.513	128.499
12	35	15	4.5	1.189	108.019	27	45	15	3	1.070	86.375
13	35	18.75	4.5	1.486	118.259	28	45	15	6	1.188	128.955
14	35	30	4.5	1.563	148.979	29	45	30	6	1.917	169.915
15	35	26.25	4.5	1.497	138.739						

The response surface approximation models for the two objective functions safety factor and structural mass with respect to the three decision variables were constructed according to Equation (12) based on the experimental data.

$$SF = 0.1395 - 0.0064x_1 + 0.0539x_2 + 0.1045x_3 + 0.0001x_1^2 -0.0023x_2^2 - 0.0288x_3^2 - 0.0002x_1x_3 + 0.0015x_2x_3 SM = 2.7307x_2 + 15.6107x_3 - 0.1575x_3^2$$
(15)

The constructed response surface approximation model was evaluated for significance according to Equation (13), and the calculated results are shown in Table **??**. From Table **??**, we can see that for the two objective functions their determinable coefficients and adjusted determinable coefficients are close to 1 and the root mean square error is close to 0, indicating that the approximate models of the two objective functions have good accuracy.

Objective Function	Decidability Factor	Adjustment of Decidability Factor	Root Mean Square Error	
SF	0.9637	0.9593	$0.0685 \ 5.05 imes 10^{-4}$	
SM	1	1		

Table 7. Significance assessment value.

The MOGA multi-objective optimization model is obtained by bringing the response surface approximation model of Equation (15) into Equation (14). The model is input into MATLAB 6.0 software, and the maximum number of iterations of MOGA is set to 500, the initial population is 60, the crossover rate and variable rate are kept as default, and finally, six split drape coupling plate are obtained. The detailed design solution Pareto solution is shown in Figure **??**.



Figure 9. Split drape coupling plate detailed design solution Pareto solution set.

Each point in the Pareto solution set satisfies the constraints. In this paper, a Pareto solution is selected based on the decision maker's preference, and its three decision variables are rounded to obtain the top coupling plate hole distance of 45 mm, the small coupling plate thickness of 18 mm, and the thickness of the equal angle steel of 5 mm as the optimal detailed design solution. The three-dimensional model is re-established using the three parameters to obtain the structural mass of 123 kg, and the mechanical analysis is carried out to obtain the distribution of the safety factor of the split drape coupling plate under 144KN load by ANSYS Workbench 12.0 software, as shown in Figure **??**, which shows that the minimum safety factor of 1.51 satisfies the constraint condition.



Figure 10. Split drape coupling plate design solution.

After getting the final detailed design plan of this split drape coupling plate, the corresponding assembly drawing and parts engineering drawing can be drawn to the next stage of product development according to the design content. The whole set of the model adopts different methods from three stages of requirement analysis, conceptual design, and detailed design. In the conceptual design process, indicators for conceptual design are set through requirements analysis, and one of the five conceptual solutions was selected through the decision-making process. In the detailed design process, three critical parameters were determined through a sample set consisting of 29 solutions. The model integrates every phase of product design and its method through decision indicators, which leads to improvement of design continuity. The model also makes the design more directional and can improve the efficiency of design.

6. Conclusions

Decision-making of product solutions can select the optimal product solution and directly improve product quality. In this study, a model is proposed to integrate the design process, decision-making method, and decision indicators. Compared with previous methods, the contributions of this method are as follows. (1) A connection between the conceptual design process and the detailed design process is proposed. With the division of function indicators and performance indicators, the conceptual design process can be transitioned to the detailed design process. (2) The hesitant fuzzy linguistic term set and entropy power method were used to improve the TOPSIS method, which can make a better decision in the decision-making process of the conceptual design solution. (3) The combination of MOGA and a 3D model is used to find the Pareto solution. It can not only fit the demands of the users but also make the indicators to the parameters of the product. Based on the proposed model, a case study on the design and decision-making of high-voltage power fixtures is conducted, and the computational process of the proposed method is presented. The simulated design solution proves that the model can make the design decision directional and maintain design continuity which is helpful for the design process.

Although this paper presents a model and method for reference, there are certain shortcomings and limitations. The authors suggest the following directions for future research. First, the interaction process between users and designers should be further explored, and it is important to focus on different fields of design, such as apparel design or complex electromechanical products design. Second, a decision database should be established for products in different fields. The decision parameters should be adjusted according to the different fields of products, such as different objective functions or different parameters of the multi-objective genetic algorithm. Third, an effective software should be developed to support the full design process and decision-making process, and new methods can be integrated into the system.

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