## Supporting Information

# Method of Moments Applied to Most-Likely HighTemperature Free-radical Polymerization Reactions 

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## Rate Equations for the Other Reactions

## 1. Propagation by tertiary radicals of type $R_{n}^{* * *}$

In this kind of propagation reaction, one monomer is added to a tertiary radical of the type $R_{n}^{* * *}$, generating a secondary radical that is one monomer unit longer than the tertiary radical. This reaction forms long branches along the backbone.

$$
\begin{align*}
& R_{n}^{* * *}+M \xrightarrow{k_{p}^{t}} R_{n+1}^{* *}  \tag{S1}\\
& r_{M}=-k_{p}^{t}[M] \sum\left[R_{n}^{* * *}\right]=-k_{p}^{t}[M] \rho_{0}^{* * *}  \tag{S2}\\
& r_{\rho_{0}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{0}\left[R_{n}^{* * *}\right]=k_{p}^{t}[M] \rho_{0}^{* * *}  \tag{S3}\\
& r_{\rho_{1}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{1}\left[R_{n}^{* * *}\right]=k_{p}^{t}[M]\left(\rho_{1}^{* * *}+\rho_{0}^{* * *}\right)  \tag{S4}\\
& r_{\rho_{2}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{2}\left[R_{n}^{* * *}\right]=k_{p}^{t}[M]\left(\rho_{2}^{* * *}+2 \rho_{1}^{* * *}+\rho_{0}^{* * *}\right)  \tag{S5}\\
& r_{\rho_{0}^{* * *}}=-k_{p}^{t}[M] \sum n^{0}\left[R_{n}^{* * *}\right]=-k_{p}^{t}[M] \rho_{0}^{* * *}  \tag{S6}\\
& r_{\rho_{1}^{* * *}}=-k_{p}^{t}[M] \sum n^{1}\left[R_{n}^{* * *}\right]=-k_{p}^{t}[M] \rho_{1}^{* * *}  \tag{S7}\\
& r_{\rho_{2}^{* * *}}=-k_{p}^{t}[M] \sum n^{2}\left[R_{n}^{* * *}\right]=-k_{p}^{t}[M] \rho_{2}^{* * *} \tag{S8}
\end{align*}
$$

Here ( $n+1$ ) in Eqs.(S3)-(S5) reflects the fact that the reaction generates a secondary radical with length $(n+1)$ monomer units, where $n$ in Eqs.(S6)-(S8) reflects the fact that the reaction consumes a tertiary radical of the type $R_{n}^{* * *}$ with length $n$ monomer units. Note that these rate equations satisfy $r_{M}+r_{\rho_{1}^{* *}}+r_{\rho_{1}^{* * *}}=$ 0 , confirming that this reaction does not change the total number of monomer units in the system.

## 2. Propagation by tertiary radicals of type $\tilde{R}_{n}^{* * *}$

In this kind of propagation reaction, one monomer is added to a tertiary radical of the type $\tilde{R}_{n}^{* * *}$, generating a secondary radical that is one monomer unit longer than the tertiary radical:

$$
\begin{equation*}
\widetilde{R}_{n}^{* * *}+M \xrightarrow{k_{p}^{t}} R_{n+1}^{* *} \tag{S9}
\end{equation*}
$$

The occurrence of this reaction leads to the formation of a short chain branch. The contributions of this reaction to the production rates of different species as well as rates of moments are as follows:

$$
\begin{align*}
& r_{M}=-k_{p}^{t}[M] \sum\left[\widetilde{R}_{n}^{* * *}\right]=-k_{p}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S10}\\
& r_{\rho_{0}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{0}\left[\widetilde{R}_{n}^{* * *}\right]=k_{p}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S11}\\
& r_{\rho_{1}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{1}\left[\widetilde{R}_{n}^{* * *}\right]=k_{p}^{t}[M]\left(\tilde{\rho}_{1}^{* * *}+\tilde{\rho}_{0}^{* * *}\right)  \tag{S12}\\
& r_{\rho_{2}^{* *}}=k_{p}^{t}[M] \sum(n+1)^{2}\left[\widetilde{R}_{n}^{* * *}\right]=k_{p}^{t}[M]\left(\tilde{\rho}_{2}^{* * *}+2 \widetilde{\rho}_{1}^{* * *}+\tilde{\rho}_{0}^{* * *}\right)  \tag{S13}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{p}^{t}[M] \sum n^{0}\left[\widetilde{R}_{n}^{* * *}\right]=-k_{p}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S14}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{p}^{t}[M] \sum n^{1}\left[\widetilde{R}_{n}^{* * *}\right]=-k_{p}^{t}[M] \tilde{\rho}_{1}^{* * *}  \tag{S15}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{p}^{t}[M] \sum n^{2}\left[\widetilde{R}_{n}^{* *}\right]=-k_{p}^{t}[M] \tilde{\rho}_{2}^{* * *} \tag{S16}
\end{align*}
$$

Note that the rate equations satisfy $r_{M}+r_{\rho_{1}^{* *}}+r_{\widetilde{\rho}_{1}^{* * *}}=0$, confirming that the reaction does not change the total number of monomer units in the system.

## 3. $\beta$-Scission reaction from the left hand side of tertiary radical type $R_{n}^{* * *}$

In this kind of $\beta$-scission reaction, there are ( $n-2$ ) possible sites for scission. Like other $\beta$-scission reactions, it produces a secondary radical and a macromonomer.

$$
\begin{align*}
& r_{\rho_{0, L}^{* * *}}=-\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right](n-2)=-\frac{1}{2} k_{\beta} \rho_{0}^{* * *}  \tag{S17}\\
& r_{\rho_{1, L}^{* *}}=-\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right] n(n-2)=-\frac{1}{2} k_{\beta} \rho_{1}^{* * *}  \tag{S18}\\
& r_{\rho_{2, L}^{* *}}=-\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right] n^{2}(n-2)=-\frac{1}{2} k_{\beta} \rho_{2}^{* * *}  \tag{S19}\\
& r_{\rho_{0, L}^{* *}}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right](n-2)=\frac{1}{2} k_{\beta} \rho_{0}^{* * *}  \tag{S20}\\
& r_{\rho_{1, L}^{* *}}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right](1+\cdots+(n-2))= \\
& \sum_{2}^{\frac{1}{2}} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right] \frac{1}{2}(n-2)(n-1)=\frac{1}{4} k_{\beta}\left(\rho_{1}^{* * *}-\rho_{0}^{* * *}\right)  \tag{S21}\\
& r_{\rho_{2, L}^{* *}}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* *}\right]\left(1^{2}+\cdots+(n-2)^{2}\right)= \\
& \sum_{2}^{\frac{1}{2}} k_{\beta}\left[R_{n}^{* * *}\right] \frac{(n-2)(n-1)(2 n-3)}{6(n-2)}=\frac{1}{12} k_{\beta}\left(2 \rho_{2}^{* * *}-5 \rho_{1}^{* * *}+3 \rho_{0}^{* * *}\right)  \tag{S22}\\
& r_{\epsilon_{0, L}}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* *}\right](n-2)=\frac{1}{2} k{ }_{\beta} \rho_{0}^{* * *}  \tag{S23}\\
& r_{\epsilon_{1, L}}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right](2+\cdots+(n-1))=
\end{align*}
$$

$$
\begin{align*}
& \sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right] \frac{1}{2}(n-2)(n+1)=\frac{1}{4} k_{\beta}\left(\rho_{1}^{* * *}+\rho_{0}^{* * *}\right)  \tag{S24}\\
& r_{\epsilon_{2}, L}=\sum \frac{1}{2} \frac{1}{n-2} k_{\beta}\left[R_{n}^{* * *}\right]\left(2^{2}+\cdots+(n-1)^{2}\right)= \\
& \quad \sum \frac{1}{2} k_{\beta}\left[R_{n}^{* * *}\right] \frac{(n-2)\left(2 n^{2}+n+3\right)}{6(n-2)}=\frac{1}{12} k_{\beta}\left(2 \rho_{2}^{* * *}+\rho_{1}^{* * *}+3 \rho_{0}^{* * *}\right) \tag{S25}
\end{align*}
$$

These equations satisfy $r_{\rho_{1}^{* * *}}+r_{\rho_{1}^{* *}}+r_{\epsilon_{1}}=0$, confirming that this reaction does not change the total number of monomer units.

## 4. Chain transfer from a tertiary radical type $R_{n}^{* * *}$ to a solvent

In this reaction, a tertiary radical formed by transfer to polymer abstracts a hydrogen from a solvent molecule, leading to the formation of a dead polymer chain and an active solvent-based radical:

$$
\begin{equation*}
R_{n}^{* * *}+S \xrightarrow{k_{t r, s}^{t}} D_{n}+R_{0}^{*} \tag{S26}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{s}=-k_{t r, s}^{t}[S] \rho_{0}^{* * *}  \tag{S27}\\
& r_{R_{0}^{*}}=k_{t r, S}^{t}[S] \rho_{0}^{* * *}  \tag{S28}\\
& r_{\rho_{0}^{* *}}=r_{\rho_{1}^{* *}}=r_{\rho_{2}^{* *}}=0  \tag{S29}\\
& r_{\rho_{0}^{* * *}}=-k_{t r, S}^{t}[S] \rho_{0}^{* * *}  \tag{S30}\\
& r_{\rho_{1}^{* * *}}=-k_{t r, S}^{t}[S] \rho_{1}^{* * *}  \tag{S31}\\
& r_{\rho_{2}^{* * *}}=-k_{t r, S}^{t}[S] \rho_{2}^{* * *}  \tag{S32}\\
& r_{\delta_{0}}=k_{t r, S}^{t}[S] \rho_{0}^{* * *}  \tag{S33}\\
& r_{\delta_{1}}=k_{t r, S}^{t}[S] \rho_{1}^{* * *}  \tag{S34}\\
& r_{\delta_{2}}=k_{t r, S}^{t}[S] \rho_{2}^{* * *} \tag{S35}
\end{align*}
$$

## 5. Chain transfer from a tertiary radical type $\widetilde{R}_{n}^{* * *}$ to a solvent

In this reaction, a tertiary radical formed through backbiting abstracts a hydrogen from a solvent molecule, resulting in the formation of a dead polymer chain and an active solvent-based radical:

$$
\begin{gather*}
\tilde{R}_{n}^{* * *}+S \xrightarrow{k_{t r, s}^{t}} D_{n}+R_{0}^{*}  \tag{S36}\\
r_{s}=-k_{t r, S}^{t}[S] \tilde{\rho}_{0}^{* * *}  \tag{S37}\\
r_{\rho_{0}^{* *}}=r_{\rho_{1}^{* *}}=r_{\rho_{2}^{* *}}=0  \tag{S38}\\
r_{\tilde{\rho}_{0}^{* *}}=-k_{t r, S}^{t}[S] \tilde{\rho}_{0}^{* * *} \tag{S39}
\end{gather*}
$$

$$
\begin{align*}
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{t r, S}^{t}[S] \tilde{\rho}_{1}^{* * *}  \tag{S40}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t r, S}^{t}[S] \tilde{\rho}_{2}^{* * *}  \tag{S41}\\
& r_{\delta_{0}}=k_{t r, S}^{t}[S] \tilde{\rho}_{0}^{* * *}  \tag{S42}\\
& r_{\delta_{1}}=k_{t r, S}^{t}[S] \tilde{\rho}_{1}^{* * *}  \tag{S43}\\
& r_{\delta_{2}}=k_{t r, S}^{t}[S] \tilde{\rho}_{2}^{* * *}  \tag{S44}\\
& r_{R_{0}^{*}}=k_{t r, S}^{t}[S] \tilde{\rho}_{0}^{* * *} \tag{S45}
\end{align*}
$$

## 6. Chain transfer from a tertiary radical type $R_{n}^{* * *}$ to a monomer

In this transfer to monomer reaction, a macroradical of type $R_{n}^{* * *}$ abstracts a hydrogen from a monomer leading to the formation of a dead polymer chain with the same number of monomer units and the generation of a secondary radical with one monomer unit:

$$
\begin{equation*}
R_{n}^{* * *}+M \xrightarrow{k_{t r, M}^{t}} D_{n}+R_{1}^{* *} \tag{S46}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{R_{1}^{* *}}=k_{t r, M}^{t}[M] \rho_{0}^{* * *}  \tag{S47}\\
& r_{M}=-k_{t r, M}^{t}[M] \rho_{0}^{* * *}  \tag{S48}\\
& r_{\rho_{0}^{* *}}=r_{\rho_{1}^{* *}}=r_{\rho_{2}^{* * *}}=k_{t r, M}^{t}[M] \rho_{0}^{* * *}  \tag{S49}\\
& r_{\rho_{0}^{* * *}}=-k_{t r, M}^{t}[M] \rho_{0}^{* * *}  \tag{S50}\\
& r_{\rho_{1}^{* * *}}^{*}=-k_{t r, M}^{t}[M] \rho_{1}^{* * *}  \tag{S51}\\
& r_{\rho_{2}^{* * *}}=-k_{t r, M}^{t}[M] \rho_{2}^{* * *}  \tag{S52}\\
& r_{\delta_{0}}=k_{t r, M}^{t}[M] \rho_{0}^{* * *}  \tag{S53}\\
& r_{\delta_{1}}=k_{t r, M}^{t}[M] \rho_{1}^{* * *}  \tag{S54}\\
& r_{\delta_{2}}=k_{t r, M}^{t}[M] \rho_{2}^{* * *} \tag{S55}
\end{align*}
$$

This reaction should does not change the total number of monomer units in the system; $r_{M}+r_{\rho_{1}^{* *}}+r_{\rho_{1}^{* * *}}+$ $r_{\delta_{1}}=0$ holds.

## 7. Chain transfer from a tertiary radical type $\tilde{R}_{n}^{* * *}$ to a monomer

In this transfer to monomer reaction, a macroradical of type $\widetilde{R}_{n}^{* * *}$ abstracts a hydrogen from a monomer leading to the formation of a dead polymer chain with the same number of monomer units and the generation of a secondary radical with one monomer unit:

$$
\begin{equation*}
\widetilde{R}_{n}^{* * *}+M \xrightarrow{k_{t r, M}^{t}} D_{n}+R_{1}^{* *} \tag{S56}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{R_{1}^{* *}}=k_{t r, M}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S57}\\
& r_{M}=-k_{t r, M}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S58}\\
& r_{\rho_{0}^{* *}}=r_{\rho_{1}^{* *}}=r_{\rho_{2}^{* *}}=k_{t r, M}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S59}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{t r, M}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S60}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{t r, M}^{t}[M] \tilde{\rho}_{1}^{* * *}  \tag{S61}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t r, M}^{t}[M] \tilde{\rho}_{2}^{* * *}  \tag{S62}\\
& r_{\delta_{0}}=k_{t r, M}^{t}[M] \tilde{\rho}_{0}^{* * *}  \tag{S63}\\
& r_{\delta_{1}}=k_{t r, M}^{t}[M] \tilde{\rho}_{1}^{* * *}  \tag{S64}\\
& r_{\delta_{2}}=k_{t r, M}^{t}[M] \tilde{\rho}_{2}^{* * *} \tag{S65}
\end{align*}
$$

As expected, this reaction does not change the total number of monomer units: $r_{M}+r_{\rho_{1}^{* *}}+r_{\tilde{\rho}_{1}^{* * *}}+r_{\delta_{1}}=$ 0.
8. Chain transfer from a tertiary radical type $R_{n}^{* * *}$ to a dead polymer chain

In this reaction, a tertiary radical of type $R_{n}^{* * *}$ abstracts a hydrogen from a dead polymer chain, leading to the formation of a new dead polymer chain and a new tertiary radical of type $R_{m}^{* * *}$ :

$$
\begin{equation*}
R_{n}^{* * *}+D_{m} \xrightarrow{m k_{t r, P}^{t}} D_{n}+R_{m}^{* * *} \tag{S66}
\end{equation*}
$$

This reaction has a reactant monoradical that is different from its counterpart in reaction (120). The reactions (S66) and (120) also differ in their rate coefficients; the rate of the reaction (S66) is around three orders of magnitude lower than that of the reaction (120). The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{\rho_{0}^{* * *}}=0  \tag{S67}\\
& r_{\rho_{1}^{* * *}}=-k_{t r, P}^{t} \rho_{1}^{* * *} \delta_{1}+k_{t r, P}^{t} \delta_{2} \rho_{0}^{* * *}  \tag{S68}\\
& r_{\rho_{2}^{* * *}}=-k_{t r, P}^{t} \rho_{2}^{* * *} \delta_{1}+k_{t r, P}^{t} \delta_{3} \rho_{0}^{* * *}  \tag{S69}\\
& r_{\delta_{0}}=0  \tag{S70}\\
& r_{\delta_{1}}=-k_{t r, P}^{t} \rho_{0}^{* * *} \delta_{2}+k_{t r, P}^{t} \delta_{1} \rho_{1}^{* * *}  \tag{S71}\\
& r_{\delta_{2}}=-k_{t r, P}^{t} \rho_{0}^{* * *} \delta_{3}+k_{t r, P}^{t} \delta_{1} \rho_{2}^{* * *} \tag{S72}
\end{align*}
$$

Again, the sum of the first moments here is zero, which confirms this reaction does not change the total number of monomer units in the system.

## 9. Chain transfer from a tertiary radical type $\tilde{R}_{n}^{* * *}$ to a dead polymer chain

In this reaction, a tertiary radical of type $\widetilde{R}_{n}^{* *}$ abstracts a hydrogen from a dead polymer chain, leading to the formation of a new dead polymer chain and a new tertiary radical of type $R_{m}^{* * *}$ :

$$
\begin{equation*}
\widetilde{R}_{n}^{* * *}+D_{m} \xrightarrow{m k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \tag{S73}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *} \delta_{1}  \tag{S74}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{t r, p}^{t} \tilde{\rho}_{1}^{* * *} \delta_{1}  \tag{S75}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t r, p}^{t} \tilde{\rho}_{2}^{* * *} \delta_{1}  \tag{S76}\\
& r_{\rho_{0}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *} \delta_{1}  \tag{S77}\\
& r_{\rho_{1}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *} \delta_{2}  \tag{S78}\\
& r_{\rho_{2}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *} \delta_{3}  \tag{S79}\\
& r_{\delta_{0}}=0  \tag{S80}\\
& r_{\delta_{1}}=-k_{t r, P}^{t} \tilde{P}_{0}^{* * *} \delta_{2}+k_{t r, P}^{t} \delta_{1} \tilde{\rho}_{1}^{* * *}  \tag{S81}\\
& r_{\delta_{2}}=-k_{t r, P}^{t} \tilde{P}_{0}^{* * *} \delta_{3}+k_{t r, P}^{t} \delta_{1} \tilde{\rho}_{2}^{* * *} \tag{S82}
\end{align*}
$$

This reaction does not change the total number of monomer units in the system either; $r_{\tilde{\rho}_{1}^{* * *}}+r_{\rho_{1}^{* * *}}+r_{\delta_{1}}=$ 0 holds.

## 10. Chain transfer from a tertiary radical type $R_{n}^{* * *}$ to a macromonomer

This is a chain transfer reaction to a macromonomer by a macroradical containing a tertiary radical of type $R_{n}^{* * *}$. The occurrence of the reaction causes the generation of the same type of tertiary radical, $R_{m}^{* * *}$, and a dead saturated polymer chain:

$$
\begin{equation*}
R_{n}^{* * *}+U_{m} \xrightarrow{(m-1) k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \tag{S83}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{\rho_{0}^{* * *}}=0  \tag{S84}\\
& r_{\rho_{1}^{* * *}}=-k_{t r, p}^{t} \rho_{1}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)+k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{2}-\epsilon_{1}\right)  \tag{S85}\\
& r_{\rho_{2}^{* * *}}=-k_{t r, p}^{t} \rho_{2}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)+k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{3}-\epsilon_{2}\right)  \tag{S86}\\
& r_{\delta_{0}}=k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S87}\\
& r_{\delta_{1}}=k_{t r, p}^{t} \rho_{1}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S88}\\
& r_{\delta_{2}}=k_{t r, p}^{t} \rho_{2}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S89}\\
& r_{\epsilon_{0}}=-k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S90}\\
& r_{\epsilon_{1}}=-k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{2}-\epsilon_{1}\right)  \tag{S91}\\
& r_{\epsilon_{2}}=-k_{t r, p}^{t} \rho_{0}^{* * *}\left(\epsilon_{3}-\epsilon_{2}\right) \tag{S92}
\end{align*}
$$

The sum of the first moments is zero here, which confirms that this reaction does not change the total number of monomer units in the system.

## 11. Chain transfer from a tertiary radical type $\tilde{R}_{n}^{* * *}$ to a macromonomer

This reaction involves the abstraction of a tertiary hydrogen by a tertiary radical of type $\widetilde{R}_{n}^{* * *}$ from a macromonomer, leading to the generation of an $R_{m}^{* * *}$-type tertiary radical and a dead saturated polymer chain:

$$
\begin{equation*}
\widetilde{R}_{n}^{* * *}+U_{m} \xrightarrow{(m-1) k_{t r r p}^{t}} D_{n}+R_{m}^{* * *} \tag{S93}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{\rho_{0}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S94}\\
& r_{\rho_{1}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{2}-\epsilon_{1}\right)  \tag{S95}\\
& r_{\rho_{2}^{* * *}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{3}-\epsilon_{2}\right)  \tag{S96}\\
& r_{\tilde{\rho}_{0}^{* * *}}^{*}=-k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S97}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{t r, p}^{t} \tilde{\rho}_{1}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S98}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t r, p}^{t} \tilde{\rho}_{2}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S99}\\
& r_{\delta_{0}}=k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S100}\\
& r_{\delta_{1}}=k_{t r, p}^{t} \tilde{\rho}_{1}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S101}\\
& r_{\delta_{2}}=k_{t r, p}^{t} \tilde{\rho}_{2}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S102}\\
& r_{\epsilon_{0}}=-k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{1}-\epsilon_{0}\right)  \tag{S103}\\
& r_{\epsilon_{1}}=-k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{2}-\epsilon_{1}\right)  \tag{S104}\\
& r_{\epsilon_{2}}=-k_{t r, p}^{t} \tilde{\rho}_{0}^{* * *}\left(\epsilon_{3}-\epsilon_{2}\right) \tag{S105}
\end{align*}
$$

The sum of the first moments is zero here, which confirms that this reaction does not change the total number of monomer units in the system.

## 12. Termination by combination of a secondary radical and a tertiary radical type $R_{m}^{* * *}$

In this reaction, a secondary radical and a tertiary radical of the type $R_{m}^{* * *}$ combine and form a saturated dead polymer chain that includes the monomer units of both radicals:

$$
\begin{equation*}
R_{n}^{* *}+R_{m}^{* * *} \xrightarrow{2 k_{t c}^{t}} D_{n+m} \tag{S106}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{R_{0}^{*}}=-2 k_{t c}^{t}\left[R_{0}^{*}\right] \rho_{0}^{* * *}  \tag{S107}\\
& r_{R_{1}^{* *}}=-2 k_{t c}^{t}\left[R_{1}^{* *}\right] \rho_{0}^{* * *} \tag{S108}
\end{align*}
$$

$$
\begin{align*}
& r_{R_{2}^{* *}}=-2 k_{t c}^{t}\left[R_{2}^{* *}\right] \rho_{0}^{* * *}  \tag{S109}\\
& r_{\rho_{0}^{* *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \rho_{0}^{* *}  \tag{S110}\\
& r_{\rho_{1}^{* *}}=-2 k_{t c}^{t} \rho_{1}^{* *} \rho_{0}^{* * *}  \tag{S111}\\
& r_{\rho_{2}^{* *}}=-2 k_{t c}^{t} \rho_{2}^{* *} \rho_{0}^{* *}  \tag{S112}\\
& r_{\rho_{0}^{* * *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S113}\\
& r_{\rho_{1}^{* * *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \rho_{1}^{* * *}  \tag{S114}\\
& r_{\rho_{2}^{* * *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \rho_{2}^{* * *}  \tag{S115}\\
& r_{\delta_{0}}=2 k_{t c}^{t} \rho_{0}^{* *} \rho_{0}^{* *}  \tag{S116}\\
& r_{\delta_{1}}=2 k_{t c}^{t}\left(\rho_{1}^{* *} \rho_{0}^{* * *}+\rho_{0}^{* *} \rho_{1}^{* * *}\right)  \tag{S117}\\
& r_{\delta_{2}}=2 k_{t c}^{t}\left(\rho_{2}^{* *} \rho_{0}^{* * *}+\rho_{0}^{* *} \rho_{2}^{* * *}+2 \rho_{1}^{* *} \rho_{1}^{* * *}\right) \tag{S118}
\end{align*}
$$

Here, $r_{\rho_{1}^{* *}}+r_{\rho_{1}^{* * *}}+r_{\delta_{1}}=0$, confirming that this reaction does not change the total number of monomer units, as it should not.

## 13. Termination by combination of a secondary radical and a tertiary radical type $\tilde{R}_{m}^{* * *}$

In this reaction, a secondary radical and a tertiary radical of the type $\widetilde{R}_{m}^{* * *}$ combine and form a saturated dead polymer chain that includes the monomer units of both radicals:

$$
\begin{equation*}
R_{n}^{* *}+\widetilde{R}_{m}^{* * *} \xrightarrow{2 k_{t c}^{t}} D_{n+m} \tag{S119}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{R_{0}^{*}}=-2 k_{t c}^{t}\left[R_{0}^{*}\right] \tilde{\rho}_{0}^{* * *}  \tag{S120}\\
& r_{R_{1}^{* *}}=-2 k_{t c}^{t}\left[R_{1}^{*}\right] \tilde{\rho}_{0}^{* * *}  \tag{S121}\\
& r_{R_{2}^{* *}}=-2 k_{t c}^{t}\left[R_{2}^{*}\right] \tilde{\rho}_{0}^{* * *}  \tag{S122}\\
& r_{\rho_{0}^{* *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S123}\\
& r_{\rho_{1}^{* *}}=-2 k_{t c}^{t} \rho_{1}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S124}\\
& r_{\rho_{2}^{* *}}=-2 k_{t c}^{t} \rho_{2}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S125}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S126}\\
& r_{\tilde{\rho}_{1}^{* *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \tilde{\rho}_{1}^{* * *}  \tag{S127}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-2 k_{t c}^{t} \rho_{0}^{* *} \tilde{\rho}_{2}^{* * *}  \tag{S128}\\
& r_{\delta_{0}}=2 k_{t c}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S129}\\
& r_{\delta_{1}}=2 k_{t c}^{t}\left(\rho_{1}^{* *} \tilde{\rho}_{0}^{* * *}+\rho_{0}^{* *} \tilde{\rho}_{1}^{* * *}\right) \tag{S130}
\end{align*}
$$

$$
\begin{equation*}
r_{\delta_{2}}=2 k_{t c}^{t}\left(\rho_{2}^{* *} \tilde{\rho}_{0}^{* * *}+\rho_{0}^{* *} \tilde{\rho}_{2}^{* * *}+2 \rho_{1}^{* *} \tilde{\rho}_{1}^{* * *}\right) \tag{S131}
\end{equation*}
$$

Here, $r_{\rho_{1}^{* *}}+r_{\tilde{\rho}_{1}^{* * *}}+r_{\delta_{1}}=0$, confirming that this reaction does not change the total number of monomer units, as it should not.

## 14. Termination by combination of two tertiary radicals of the types $R_{n}^{* * *}$ and $\tilde{R}_{m}^{* * *}$

In this reaction, a tertiary radical of the type $R_{n}^{* * *}$ and a tertiary radical of the type $\widetilde{R}_{m}^{* * *}$ combine and form a saturated dead polymer chain that includes the monomer units of both radicals. The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& R_{n}^{* * *}+\widetilde{R}_{m}^{* * *} \xrightarrow{2 k_{c t}^{t}} D_{n+m}  \tag{S132}\\
& r_{\rho_{0}^{* * *}}=-2 k_{t c}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S133}\\
& r_{\rho_{1}^{* * *}}=-2 k_{t c}^{t t} \rho_{1}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S134}\\
& r_{\rho_{2}^{* * *}}^{*}=-2 k_{t c}^{t t} \rho_{2}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S135}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-2 k_{t c}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S136}\\
& r_{\tilde{\rho}_{1}}^{* * *}=-2 k_{t c}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{1}^{* * *}  \tag{S137}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-2 k_{t c}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{2}^{* * *}  \tag{S138}\\
& r_{\delta_{0}}=2 k_{t c}^{t t} p_{0}^{* * *} \tilde{\rho}_{0}^{* *}  \tag{S139}\\
& r_{\delta_{1}}=2 k_{t c}^{t t}\left(\rho_{1}^{* * *} \tilde{\rho}_{0}^{* * *}+\rho_{0}^{* * *} \rho_{1}^{* * *}\right)  \tag{S140}\\
& r_{\delta_{2}}=2 k_{t c}^{t t}\left(\rho_{2}^{* * *} \tilde{\rho}_{0}^{* * *}+\rho_{0}^{\left.* * * \tilde{\rho}_{2}^{* * *}+2 \rho_{1}^{* * *} \tilde{\rho}_{1}^{* * *}\right)}\right. \tag{S141}
\end{align*}
$$

The sum of the first moments is zero, confirming that there is no change in the total number of monomer units upon the occurrence of this reaction.

## 15. Termination by disproportionation of a secondary radical and a tertiary radical of the type $R_{m}^{* * *}$

In these reactions, a secondary radical abstracts a hydrogen from or donates a hydrogen to a tertiary radical of type $R_{m}^{* * *}$, leading to the formation of a saturated and an unsaturated dead chain:

$$
\begin{align*}
& R_{n}^{* *}+R_{m}^{* * *} \xrightarrow{k_{t d}^{t}} D_{n}+U_{m}  \tag{S142}\\
& R_{n}^{* *}+R_{m}^{* * *} \xrightarrow{k_{t d}^{t}} D_{m}+U_{n} \tag{S143}
\end{align*}
$$

Relations to calculated $k_{t d}^{t}$ from $k_{t}$ and $k_{t}^{t t}$ have been reported in Ref. [1]. The following rate equations describe the contributions of this reaction of (S142) to the production and consumption of different species as well as the relevant moments:

$$
\begin{gather*}
r_{R_{0}^{*}}=-k_{t d}^{t}\left[R_{0}^{*}\right] \rho_{0}^{* * *}  \tag{S144}\\
r_{R_{1}^{* *}}=-k_{t d}^{t}\left[R_{1}^{* *}\right] \rho_{0}^{* * *}  \tag{S145}\\
r_{R_{2}^{* *}}=-k_{t d}^{t}\left[R_{2}^{* *}\right] \rho_{0}^{* * *} \tag{S146}
\end{gather*}
$$

$$
\begin{align*}
& r_{\rho_{0}^{* *}}=-k_{t d}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S147}\\
& r_{\rho_{1}^{* *}}=-k_{t d}^{t} \rho_{1}^{* *} \rho_{0}^{* * *}  \tag{S148}\\
& r_{\rho_{2}^{* *}}=-k_{t d}^{t} \rho_{2}^{* *} \rho_{0}^{* * *}  \tag{S149}\\
& r_{\rho_{0}^{* * *}}=-k_{t d}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S150}\\
& r_{\rho_{1}^{* * *}}=-k_{t d}^{t} \rho_{0}^{* *} \rho_{1}^{* *}  \tag{S151}\\
& r_{\rho_{2}^{* * *}}=-k_{t d}^{t} \rho_{0}^{* *} \rho_{2}^{* * *}  \tag{S152}\\
& r_{\delta_{0}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S153}\\
& r_{\delta_{1}}=k_{t d}^{t} \rho_{1}^{* *} \rho_{0}^{* * *}  \tag{S154}\\
& r_{\delta_{2}}=k_{t d}^{t} \rho_{2}^{* *} \rho_{0}^{* * *}  \tag{S155}\\
& r_{\epsilon_{0}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S156}\\
& r_{\epsilon_{1}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{1}^{* * *}  \tag{S157}\\
& r_{\epsilon_{2}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{2}^{* * *} \tag{S158}
\end{align*}
$$

As in the case of the other reactions, for the reaction of (S142), the sum of the first moments is zero here too. For the reaction of (S143), the rate equations of (S144) to (S154) are applicable. However, the following rate equations are different:

$$
\begin{align*}
& r_{\delta_{1}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{1}^{* * *}  \tag{S159}\\
& r_{\delta_{2}}=k_{t d}^{t} \rho_{0}^{* *} \rho_{2}^{* * *}  \tag{S160}\\
& r_{\epsilon_{0}}= k_{t d}^{t} \rho_{0}^{* *} \rho_{0}^{* * *}  \tag{S161}\\
& r_{\epsilon_{1}}=k_{t d}^{t} \rho_{1}^{* *} \rho_{0}^{* * *}  \tag{S162}\\
& r_{\epsilon_{2}}=k_{t d}^{t} \rho_{2}^{* *} \rho_{0}^{* *} \tag{S163}
\end{align*}
$$

16. Termination by disproportionation of a secondary and a tertiary radical of the type $\tilde{R}_{m}^{* * *}$

In these reactions, a secondary radical abstracts a hydrogen from or donates a hydrogen to a tertiary radical of the type $\widetilde{R}_{m}^{* * *}$, leading to the formation of a saturated and an unsaturated dead chain:

$$
\begin{align*}
& R_{n}^{* *}+\widetilde{R}_{m}^{* * *} \xrightarrow{k_{t d}^{t}} D_{m}+U_{n}  \tag{S164}\\
& R_{n}^{* *}+\widetilde{R}_{m}^{* * *} \xrightarrow{k_{t d}^{t}} D_{n}+U_{m} \tag{S165}
\end{align*}
$$

The following rate equations describe the contributions of the reaction (S164) to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{R_{0}^{*}}=-k_{t d}^{t}\left[R_{0}^{*}\right] \tilde{\rho}_{0}^{* * *}  \tag{S166}\\
& r_{R_{1}^{* *}}=-k_{t d}^{t}\left[R_{1}^{* *}\right] \tilde{\rho}_{0}^{* * *} \tag{S167}
\end{align*}
$$

$$
\begin{align*}
& r_{R_{2}^{* *}}=-k_{t d}^{t}\left[R_{2}^{* *}\right] \tilde{\rho}_{0}^{* * *}  \tag{S168}\\
& r_{\rho_{0}^{* *}}=-k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S169}\\
& r_{\rho_{1}^{* *}}=-k_{t d}^{t} \rho_{1}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S170}\\
& r_{\rho_{2}^{* *}}=-k_{t d}^{t} \rho_{2}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S171}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* *}  \tag{S172}\\
& r_{\tilde{\rho}_{1}^{* *}}=-k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{1}^{* *}  \tag{S173}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{2}^{* * *}  \tag{S174}\\
& r_{\delta_{0}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* *}  \tag{S175}\\
& r_{\delta_{1}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{1}^{* * *}  \tag{S176}\\
& r_{\delta_{2}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{2}^{* * *}  \tag{S177}\\
& r_{\epsilon_{0}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S178}\\
& r_{\epsilon_{1}}=k_{t d}^{t} \rho_{1}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S179}\\
& r_{\epsilon_{2}}=k_{t d}^{t} \rho_{2}^{* *} \tilde{\rho}_{0}^{* * *} \tag{S180}
\end{align*}
$$

Again, the sum of all rates of the first moments is zero, confirming this reaction does not change the total number of monomer units in the system. For the reaction of (S165), the rate equations of (S166) to (S175) are applicable. However, the following rate equations are different:

$$
\begin{align*}
& r_{\delta_{1}}=k_{t d}^{t} \rho_{1}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S181}\\
& r_{\delta_{2}}=k_{t d}^{t} \rho_{2}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S182}\\
& r_{\epsilon_{0}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{0}^{* * *}  \tag{S183}\\
& r_{\epsilon_{1}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{1}^{* * *}  \tag{S184}\\
& r_{\epsilon_{2}}=k_{t d}^{t} \rho_{0}^{* *} \tilde{\rho}_{2}^{* * *} \tag{S185}
\end{align*}
$$

17. Termination by disproportionation between two tertiary radicals; $\left(R_{m}^{* * *}\right)$ and $\left(\tilde{R}_{n}^{* * *}\right)$

In these reactions, a tertiary radical of the type $R_{m}^{* * *}$ abstracts a hydrogen from or donates a hydrogen to a tertiary radical of the type $\widetilde{R}_{n}^{* * *}$, leading to the formation of a saturated and an unsaturated dead chain:

$$
\begin{align*}
& \widetilde{R}_{n}^{* * *}+R_{m}^{* * *} \xrightarrow{k_{t t}^{t t}} D_{m}+U_{n}  \tag{S186}\\
& \widetilde{R}_{n}^{* * *}+R_{m}^{* * *} \xrightarrow{k_{t t}^{t t}} D_{n}+U_{m} \tag{S187}
\end{align*}
$$

The following rate equations describe the contributions of the reaction of (S186) to the production and consumption of different species as well as the relevant moments:

$$
\begin{equation*}
r_{\rho_{0}^{* * *}}=-k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *} \tag{S188}
\end{equation*}
$$

$$
\begin{align*}
& r_{\rho_{1}^{* *}}=-k_{t d}^{t t} \rho_{1}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S189}\\
& r_{\rho_{2}^{* *}}=-k_{t d}^{t t} \rho_{2}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S190}\\
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* *}  \tag{S191}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{1}^{* * *}  \tag{S192}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{2}^{* * *}  \tag{S193}\\
& r_{\delta_{0}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S194}\\
& r_{\delta_{1}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{1}^{* * *}  \tag{S195}\\
& r_{\delta_{2}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{2}^{* * *}  \tag{S196}\\
& r_{\epsilon_{0}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S197}\\
& r_{\epsilon_{1}}=k_{t d}^{t t} \rho_{1}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S198}\\
& r_{\epsilon_{2}}=k_{t d}^{t t} \rho_{2}^{* * *} \tilde{\rho}_{0}^{* * *} \tag{S199}
\end{align*}
$$

The sum of rates of all first moments is zero here, which confirms that the reaction does not change the total number of monomer units in the system. For the reaction of (S187), the rate equations of (S188) to (S194) are applicable. However, the following rate equations are different:

$$
\begin{align*}
& r_{\delta_{1}}=k_{t d}^{t t} \rho_{1}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S200}\\
& r_{\delta_{2}}=k_{t d}^{t t} \rho_{2}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S201}\\
& r_{\epsilon_{0}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{0}^{* * *}  \tag{S202}\\
& r_{\epsilon_{1}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{1}^{* *}  \tag{S203}\\
& r_{\epsilon_{2}}=k_{t d}^{t t} \rho_{0}^{* * *} \tilde{\rho}_{2}^{* * *} \tag{S204}
\end{align*}
$$

18. Propagation of a tertiary radical of the type $R_{n}^{* * *}$ by reacting with a macromonomer

In this reaction, a tertiary radical of the type $R_{n}^{* * *}$ reacts with a macromonomer (unsaturated dead polymer) and propagates (forms a longer branched growing chain):

$$
\begin{equation*}
R_{n}^{* * *}+U_{m} \xrightarrow{k_{m a c}^{t}} R_{n+m}^{* * *} \tag{S205}
\end{equation*}
$$

The following rate equations describe the contributions of this reaction to the production and consumption of different species as well as the relevant moments:

$$
\begin{align*}
& r_{\rho_{0}^{* * *}=0}  \tag{S206}\\
& r_{\rho_{1}^{* * *}}=k_{\text {mac }}^{t} \rho_{0}^{* * *} \epsilon_{1}  \tag{S207}\\
& r_{\rho_{2}^{* * *}}=k_{\text {mac }}^{t}\left(\rho_{0}^{* * *} \epsilon_{2}+2 \rho_{1}^{* * *} \epsilon_{1}\right)  \tag{S208}\\
& r_{\epsilon_{0}}=-k_{\text {mac }}^{t} \rho_{0}^{* * *} \epsilon_{0}  \tag{S209}\\
& r_{\epsilon_{1}}=-k_{\text {mac }}^{t} \rho_{0}^{* * *} \epsilon_{1} \tag{S210}
\end{align*}
$$

$$
\begin{equation*}
r_{\epsilon_{2}}=-k_{m a c}^{t} \rho_{0}^{* * *} \epsilon_{2} \tag{S211}
\end{equation*}
$$

Here, $r_{\epsilon_{1}}+r_{\rho_{1}^{* * *}}=0$, confirming that the reaction does not alter the total number of monomer units in the system.

## 19. Propagation of a tertiary radical of type $\tilde{R}_{n}^{* * *}$ by reacting with a macromonomer

In this kind of propagation, a tertiary live chain $\tilde{R}_{n}^{* * *}$ reacts with a macromonomer (dead polymer chain with a double bond) and forms a tertiary radical of the type $R_{n}^{* * *}$ :

$$
\begin{equation*}
\tilde{R}_{n}^{* * *}+U_{m} \xrightarrow{k_{m a c}^{t}} R_{n+m}^{* * *} \tag{S212}
\end{equation*}
$$

The contributions of this reaction to the rates of the moments are as follows.

$$
\begin{align*}
& r_{\tilde{\rho}_{0}^{* * *}}=-k_{\text {mac }}^{t} \tilde{\rho}_{0}^{* * *} \epsilon_{0}  \tag{S213}\\
& r_{\tilde{\rho}_{1}^{* * *}}=-k_{\text {mac }}^{t} \tilde{\rho}_{1}^{* * *} \epsilon_{0}  \tag{S214}\\
& r_{\tilde{\rho}_{2}^{* * *}}=-k_{\text {mac }}^{t} \tilde{\rho}_{2}^{* * *} \epsilon_{0}  \tag{S215}\\
& r_{\rho_{0}^{* * *}}=k_{\text {mac }}^{t} \tilde{\rho}_{0}^{* * *} \epsilon_{0}  \tag{S216}\\
& r_{\rho_{1}^{* * *}}=k_{\text {mac }}^{t}\left(\tilde{\rho}_{1}^{* * *} \epsilon_{0}+\tilde{\rho}_{0}^{* * *} \epsilon_{1}\right)  \tag{S217}\\
& \left.r_{\rho_{2}^{* * *}}=k_{\text {mac }}^{t} \tilde{\rho}_{2}^{* * *} \epsilon_{0}+\tilde{\rho}_{0}^{* * *} \epsilon_{2}+2 \tilde{\rho}_{1}^{* *} \epsilon_{1}\right)  \tag{S218}\\
& r_{\epsilon_{0}}=-k_{\text {mac }}^{t} \tilde{\rho}_{0}^{* * *} \epsilon_{0}  \tag{S219}\\
& r_{\epsilon_{1}}=-k_{\text {mac }}^{t} \tilde{\rho}_{0}^{* * *} \epsilon_{1}  \tag{S220}\\
& r_{\epsilon_{2}}=-k_{\text {mac }}^{t} \tilde{\rho}_{0}^{* * *} \epsilon_{2} \tag{S221}
\end{align*}
$$

## 20. Ranges of unavailble MA rate coefficients based on the family-type-behavior

To use the famility-type behavior [2,3], one needs to find a scale factor, which in this case, is the ratio of the propagation rate coefficeint of MA to that of $n \mathrm{BA}$ or the ratio of their termination rate coefficients. As different rate coefficients have been reported for the propagation reaction of $n \mathrm{BA}$ (Table S2), several scale factors can be obtained [3]. Furthermore, for other nBA secondary reactions such as backbiting and $\beta$-scission reactions, various rate coefficients have been reported. Using the steps described below we calculated ranges for the activation energy and frequecny factor of MA $\beta$-scission rate coefficients. We used the same steps to calculate the same ranges for the MA backbiting reaction.

1. Based on family-type-behavior:

$$
\begin{equation*}
k_{\beta S_{M A}}=\frac{k_{p_{M A}}}{k_{P_{B A}}} * k_{\beta S_{B A}} \tag{S222}
\end{equation*}
$$

where $k_{\beta S_{M A^{\prime}}} k_{p_{M A^{\prime}}}, k_{P_{B A}}$ and $k_{\beta S_{B A}}$ are the $\beta$-scission rate coefficient of MA, the propagation rate coefficient of MA, the propagation rate coefficient of $n \mathrm{BA}$, and the $\beta$-Scission rate coefficient of $n B A$, respectively. Therefore:

$$
\begin{gather*}
k_{\beta S_{M A}}=\frac{z_{P_{M A}}}{z_{p_{B A}}} \frac{\exp \left(-\frac{E_{P_{M A}}}{R T}\right)}{\exp \left(-\frac{E_{P_{B A}}}{R T}\right)} * z_{\beta S_{B A}} * \exp \left(-\frac{E_{\beta S_{B A}}}{R T}\right)=\frac{z_{P_{M A}} * z_{\beta S_{B A}}}{z_{p_{B A}}} \exp \left(\frac{-E_{P_{M A}}-E_{\beta S_{B A}}+E_{P_{B A}}}{R T}\right)  \tag{S223}\\
k_{\beta S_{M A}}=\frac{z_{P_{M A}}{ }^{* z_{\beta}} S_{B A}}{z_{p_{B A}}} \exp \left(\frac{-\left(E_{P_{M A}}+E_{\beta S_{B A}}-E_{P_{B A}}\right)}{R T}\right)=z_{\beta S_{M A}} * \exp \left(\frac{-E_{\beta S_{M A}}}{R T}\right) \tag{S224}
\end{gather*}
$$

2. Calculate the upper and lower limits using:

$$
\begin{align*}
& \text { Upper limit of } z_{\beta S_{M A}}=\frac{z_{P_{M A}} \times \text { highest reported } z_{\beta S_{B A}}}{\text { lowest reported } z_{p_{B A}}}  \tag{S225}\\
& \text { Lower limit of } z_{\beta S_{M A}}=\frac{z_{P_{M A}} \times \text { lowest reported } z_{\beta S_{B A}}}{\text { highest reported } z_{p_{B A}}} \tag{S226}
\end{align*}
$$

Upper limit of $E_{\beta S_{M A}}=$ highest reported $E_{\beta S_{B A}}+E_{P_{M A}}$ - lowest reported $E_{P_{B A}}$
Lower limit of $E_{\beta S_{M A}}=E_{P_{M A}}+$ lowest reported $E_{\beta_{S B A}}-$ highest reported $E_{P_{B A}}$
The $g a$ command of MATLAB searches within these ranges to find the optimum values of unavailable MA rate coefficients at each temperature. The gel effect parameters [3] are also estimated by $g a$ command and the values are reported in Table S3. The estimated reaction kineteic parameters are then used in our polymerization reactor model to predict monomer conversion and average molecular weights.

Table S1: Most-Likely Reactions in High-Temperature Polymerization of Alkyl Acrylates.

| Monomer self-initiation $3 M \xrightarrow{k_{i}} R_{1}^{* *}+R_{2}^{* *}$ | $\begin{aligned} & \text { Backbiting } \\ & R_{n}^{* *} \xrightarrow{k_{b b}} \tilde{R}_{n}^{* * *} \end{aligned}$ | Chain transfer to polymer $\begin{aligned} & R_{n}^{* *}+D_{m} \xrightarrow{m k_{t r, P}} D_{n}+R_{m}^{* * *} \\ & R_{n}^{* * *}+D_{m} \xrightarrow{m k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \\ & \tilde{R}_{n}^{* * *}+D_{m} \xrightarrow{m k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \end{aligned}$ |
| :---: | :---: | :---: |
| Propagation $\begin{gathered} R_{n}^{* *}+M \xrightarrow{k_{p}} R_{n+1}^{* *} \\ R_{n}^{* * *}+M \xrightarrow{k_{n}^{t}} R_{n+1}^{* *} \\ \tilde{R}_{n}^{* * *}+M \xrightarrow{k_{\rightarrow}^{t}} R_{n+1}^{* *} \\ R_{n}^{* *}+U_{m} \xrightarrow{k_{\text {mac }}} R_{n+m}^{* * *} \\ R_{n}^{* * *}+U_{m} \xrightarrow{k_{\text {mac }}^{t}} R_{n+m}^{* * *} \\ \tilde{R}_{n}^{* * *}+U_{m} \xrightarrow{k_{\text {mac }}^{t}} R_{n+m}^{* *} \end{gathered}$ | $\beta$-Scission $\begin{aligned} & \tilde{R}_{n}^{* * *} \\ & \tilde{R}_{n}^{* * *} \xrightarrow{k_{\beta}} R_{2}^{* *}+U_{n-2}^{* *}+U_{3} \\ & R_{n}^{* * *} \xrightarrow{k_{\beta}} R_{m}^{* *}+U_{n-m} \\ & R_{n}^{* * *} \xrightarrow{k_{\beta}} R_{n-m}^{* *}+U_{m} \\ & \underset{\text { Migration }}{\tilde{R}_{n}^{* * *}} \xrightarrow{k_{\text {mig }}} R_{n}^{* * *} \end{aligned}$ | Termination by disproportionation |


| Chain transfer to monomer $\begin{aligned} & R_{n}^{* *}+M \xrightarrow{k_{t r, m}^{t}} D_{n}+R_{1}^{* *} \\ & R_{n}^{* * *}+M \xrightarrow{k_{t r, M}^{t}} D_{n}+R_{1}^{* *} \\ & \tilde{R}_{n}^{* * *}+M \xrightarrow{k_{t r, M}^{t}} D_{n}+R_{1}^{* *} \end{aligned}$ | Termination by combination $\begin{aligned} & R_{n}^{* *}+R_{m}^{* *} \xrightarrow{k_{t c}} D_{n+m} \\ & R_{n}^{* *}+R_{m}^{* * *} \xrightarrow{2 k_{t c}^{t}} D_{n+m} \\ & R_{n}^{* *}+\tilde{R}_{m}^{* * *} \xrightarrow{2 k_{t c}^{t}} D_{n+m} \end{aligned}$ | De-propagation $R_{n+1}^{* *} \xrightarrow{k_{-p}} R_{n}^{* *}+M$ |
| :---: | :---: | :---: |
| Chain transfer to macromonomer $\begin{aligned} & R_{n}^{* *}+U_{m} \xrightarrow{(m-1) k_{t r, p}} D_{n}+R_{m}^{* * *} \\ & R_{n}^{* * *}+U_{m} \xrightarrow{(m-1) k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \\ & \tilde{R}_{n}^{* * *}+U_{m} \xrightarrow{(m-1) k_{t r, p}^{t}} D_{n}+R_{m}^{* * *} \end{aligned}$ | $\begin{aligned} & R_{n}^{* * *}+R_{m}^{* * *} \xrightarrow{k_{t c t}^{t t}} D_{n+m} \\ & R_{n}^{* * *}+\tilde{R}_{m}^{* * *} \xrightarrow{2 k_{t c}^{t t}} D_{n+m} \\ & \tilde{R}_{n}^{* * *}+\tilde{R}_{m}^{* * *} \xrightarrow{k_{t c}^{t t}} D_{n+m} \end{aligned}$ | Chain transfer to solvent $\begin{aligned} & R_{n}^{* *}+S \xrightarrow{k_{t r, s}} D_{n}+R_{0}^{*} \\ & R_{n}^{* * *}+S \xrightarrow{k_{t r, s}^{t}} D_{n}+R_{0}^{*} \\ & \tilde{R}_{n}^{* * *}+S \xrightarrow{k_{t r, s}^{t}} D_{n}+R_{0}^{*} \end{aligned}$ |

Table S2: Kinetic Parameter Values Reported for nBA in the Literature.

| Propagation by secondary | Activation Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor (L. $\mathrm{mol}^{-1} \mathrm{~s}^{-1}$ ) | Temp. $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ref. [1] | 17.90 | 2.21E7 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 17.80 | 2.05 E 7 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 17.90 | 2.21 E 7 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [6] | 17.40 | 1.80 E 7 | 138 | Xylene | Free-Radical | 2004 |
| Ref. [7] | 17.90 | 2.21 E 7 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 17.90 | 2.21 E 7 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 17.90 | 2.21 E 7 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 17.90 | 2.21 E 7 | 60 | THF | Free-Radical | 2015 |
| Ref. [11] | 17.90 | 2.21 E 7 | 70 | Xylene | Free-Radical | 2014 |
| Ref. [12] | 17.90 | 2.21 E 7 | 50 | Bulk | Free-Radical | 2016 |
| Ref. [12] | 17.98 | 2.19 E 7 | 50 | Toluene | Free-Radical | 2016 |
| Ref. [13] | 17.24 | 1.80 E 7 | 138 | Xylene | Free-Radical | 2010 |
| Ref. [14] | 18.10 | 2.31 E 7 | 90-120 | DMF/DMSO | NMP | 2011 |
| Propagation by Tertiary | Activation <br> Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor (L. $\mathrm{mol}^{-1} \mathrm{~s}^{-1}$ ) | Temp. $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 28.60 | 1.20 E 6 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 29.50 | 1.25 E 6 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 28.90 | 1.52 E 6 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [7] | 28.60 | 1.20E6 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 28.90 | 1.58 E 6 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 28.90 | 1.58 E 6 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 28.60 | 1.20 E 6 | 60 | THF | Free-Radical | 2015 |
| Ref. [11] | 28.90 | 1.58 E 6 | 70 | Xylene | Free-Radical | 2014 |
| Ref. [15] | 28.30 | 9.20 E 5 | 60 | Toluene | Free-Radical | 2010 |
| Ref. [14] | 28.90 | 1.52 E 6 | 90-120 | DMF/DMSO | NMP | 2011 |
| Backbiting | Activation <br> Energy (kJ.mol-1 ${ }^{-1}$ ) | Frequency Factor ( $\mathrm{s}^{-1}$ ) | Temp. $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 32.70 | 7.41 E 7 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 29.80 | 4.31 E 7 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 31.70 | 4.84 E 7 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [7] | 32.70 | 7.41 E 7 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |


| Ref. [8] | 52.30 | 3.2E10 | 60 | Toluene | RAFT | 2016 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ref. [9] | 52.30 | 3.2E10 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 32.70 | 7.41 E 7 | 60 | THF | Free-Radical | 2015 |
| Ref. [15] | 34.70 | 1.60 E 8 | 60 | Toluene | Free-Radical | 2010 |
| Ref. [14] | 29.30 | 3.50E7 | 90-120 | DMSO/DMF | NMP | 2011 |
| Ref. [16] | $30.6 \pm 5.4$ | $\operatorname{Ln}(17.8 \pm 2.1)$ | 30-50 | Bulk/Propionate | Free-Radical | 2019 |
| $\beta$-Scission | Activation Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor ( $\mathrm{s}^{-1}$ ) | Temp. ( ${ }^{\circ} \mathrm{C}$ ) | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 63.90 | 1.49 E 9 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [16] | $81.10 \pm 18.2$ | $\operatorname{Ln}(29.7 \pm 5.5)$ | 110-140 | Bulk/Propionate | Free radical | 2019 |
| Ref. [7] | 63.90 | 1.49 E 9 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 55.40 | 1.47 E 9 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 55.40 | 1.47 E 9 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [14] | 71.50 | 8.60 E 10 | 90-120 | DMSO/DMF | NMP | 2011 |
|  |  |  |  |  |  |  |
| Transfer to Polymer | Activation Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor (L. $\mathrm{mol}^{-1} . \mathrm{s}^{-1}$ ) | Temp. $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 29.00 | 4.01 E 3 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 29.00 | 4.01 E 3 | 40 | NA | Free-Radical | 2003 |
| Ref. [7] | 29.00 | 4.01 E 3 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 43.30 | 6.70E7 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 27.70 | 2.48 E 3 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 29.00 | 4.01 E 3 | 60 | THF | Free-Radical | 2015 |
| Ref. [11] | 27.70 | 2.48 E 3 | 70 | Xylene | Free-Radical | 2014 |
| Transfer to monomer | Activation Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor (L. $\mathrm{mol}^{-1} . \mathrm{s}^{-1}$ ) | Temp. ( ${ }^{\circ} \mathrm{C}$ ) | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 32.60 | 2.9 E 5 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 32.60 | 2.9E5 | 40 | NA | Free-Radical | 2003 |
| Ref. [4] (by tertiary radical) | 46.10 | 2.0E5 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 32.60 | 2.9E5 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [5] (by tertiary radical) | 46.10 | 2.0E5 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [7] | 32.60 | 2.9E5 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 32.60 | 2.88 E 5 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 32.60 | 2.88 E 5 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 32.60 | 2.90 E 5 | 60 | THF | Free-Radical | 2015 |
| Ref. [11] | 32.60 | 2.88 E 5 | 70 | Xylene | Free-Radical | 2014 |
| Ref. [10] (by tertiary radical) | 46.10 | 2.00 E 5 | 60 | THF | Free-Radical | 2015 |
| Ref. [13] | 32.60 | 2.88 E 5 | 138 | Xylene | Free-Radical | 2010 |
| Termination by Secondary | Activation Energy (kJ.mol ${ }^{-1}$ ) | Frequency Factor (L. $\mathrm{mol}^{-1} . \mathrm{s}^{-1}$ ) | Temp. $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |


| Ref. [1] | 8.40 | 3.89E9 | 140-220 | Bulk | Free-Radical | 2016 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ref. [4] | 5.58 | 2.50 E 8 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 5.60 | 1.34 E 9 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [6] | 2.40 | 2.57E8 | 138 | Xylene | Free-Radical | 2004 |
| Ref. [7] | 8.40 | 3.89E9 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 8.40 | 1.30 E 10 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 3.50 | 1.32 E 10 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 8.40 | 1.30 E 10 | 60 | THF | Free-Radical | 2015 |
| Ref. [11] | 8.40 | 1.30 E 10 | 70 | Xylene | Free-Radical | 2014 |
| Ref. [15] | 8.40 | 1.30 E 10 | 60 | Toluene | Free-Radical | 2010 |
| Ref. [13] | 3.98 | 5.14E8 | 138 | Xylene | Free-Radical | 2010 |
| Termination by Tertiary | Activation Energy (kJ.mol-1 $)$ | Frequency Factor (L.mol ${ }^{-1} . \mathrm{s}^{-1}$ ) | Temp. <br> $\left({ }^{\circ} \mathrm{C}\right)$ | Polymerization Medium | Polymerization Mechanism | Publication Year |
| Ref. [1] | 19.60 | 5.30 E 9 | 140-220 | Bulk | Free-Radical | 2016 |
| Ref. [4] | 5.56 | 2.10 E 8 | 40 | NA | Free-Radical | 2003 |
| Ref. [5] | 5.60 | 1.80 E 7 | -10-30 | Bulk | Free-Radical | 2007 |
| Ref. [7] | 19.60 | 5.30 E 9 | 80-170 | Xylene/Ethyl Benzene | Free-Radical | 2010 |
| Ref. [8] | 19.60 | 5.30E9 | 60 | Toluene | RAFT | 2016 |
| Ref. [9] | 4.00 | 1.29 E 7 | 60-140 | Bulk/Xylene | Free-Radical | 2016 |
| Ref. [10] | 5.60 | 1.80 E 7 | 60 | THF | Free-Radical | 2015 |

Table S3: Estimated parameters of the gel effect model [3]

| $i$ | $b_{i}$ | $c_{i}$ |
| :---: | :---: | :---: |
| 1 | 49.805 | 0.600 |
| 2 | -10.380 | 1.750 |
| 3 | 26.140 | -0.042 |

Table S4: Equations, initial conditions, and other MA rate coefficients

| Reaction | Rate equation | Comment |
| :---: | :---: | :---: |
| Propagation of tertiary radicals $\left(k_{p}^{t}\right)$ | $k_{p}^{t}=k_{p} / 1000$ | Three orders of magnitude less than <br> propagation by secondary radicals [2] |
| Chain transfer to monomer from secondary <br> radicals $\left(k_{t r, M}\right)$ | $k_{t r, M}=b^{*} k_{t r, M}$ of $n$-BA | $b$ is a scaling factor defined in ref. [3] |
| Chain transfer to monomer from tertiary <br> radicals $\left(k_{t r, M}^{t}\right)$ | $k_{t r, M}^{t}=b * k_{t r, M}^{t}$ of $n$-BA | $b$ is a scaling factor defined in ref. [3] |
| Chain transfer to polymer from secondary <br> radical $\left(k_{t r, p}\right)$ | $k_{t r, P}=b^{*} k_{t r, P}$ of $n$-BA | $b$ is a scaling factor defined in ref. [3] |
| Chain transfer to polymer from tertiary <br> radical $\left(k_{t r, M}^{p}\right)$ | $k_{t r, p}^{t}=k_{t r, p} / 1000$ | Three orders of magnitude less than <br> corresponding secondary radical rate <br> coefficient |
| Termination of secondary radicals $\left(k_{t}\right)$ | $\log k_{t}=9.48-\frac{454}{T}$ | Reported in [17] |


| Termination of tertiary radicals $\left(k_{t}^{t}\right)$ | $k_{t}^{t}=a * k_{t}^{t}$ of $n$-BA | $a$ is a scaling factor defined in ref. [3] |  |
| :---: | :---: | :---: | :---: |
| Other equations |  |  |  |
| $k_{t}^{t t}=k_{t d}^{t t}+k_{t c}^{t t}$ | $k_{t}^{t}=k_{t d}^{t}+k_{t c}^{t}$ | $k_{t}=k_{t d}+k_{t c}$ |  |
| $k_{t d}=\delta_{t} k_{t}$ | $k_{t d}^{t t}=\delta_{t} k_{t}^{t t}$ | $k_{t d}^{t}=\delta_{s t} \sqrt{k_{t} k_{t}^{t t}}$ |  |
| $k_{t c}=\left(1-\delta_{s}\right) k_{t}$ | $k_{t c}^{t t}=\left(1-\delta_{t}\right) k_{t}^{t t}$ | $k_{t c}^{t}=\left(1-\delta_{s t}\right) \sqrt{k_{t} k_{t}^{t t}}$ |  |
| $k_{m a c}=\gamma k_{p}$ | $\delta_{s}=0.1$ | $\delta_{s t}=0.7$ |  |
| $\delta_{t}=0.9$ | $\gamma=0.5$ | All other concentrations $=0$ |  |
|  |  |  |  |
| Initial monomer concentration = 11.03 $\frac{\text { mol }}{L}$ | Polymerization time $=$ <br> $250 ~ m i n ~$ |  |  |

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