



# **Development and Applications of 3D Printing-Processed Auxetic Structures for High-Velocity Impact Protection: A Review**

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**Abstract:** Auxetic structures (AXSs) are a novel class of materials with unique mechanical deformation behavior associated with negative Poisson ratio. The combination of AXS configurations with various types of materials has unveiled a wide field of applications, including military high-velocity protection against explosions and ballistic projectiles. However, the characteristic geometric re-entrant model of AXSs imposes limitations and difficulties when using conventional manufacturing methods to assemble the structure lattice. Additive manufacturing (AM) has recently been explored as a more efficient and cost-effective method to fabricate AXSs, regardless of the type of material. This review paper focuses on the development and applications of AM processed AXSs. The review highlights the significance and great potential for this class of materials that can be produced relatively fast and at a low cost. The advantages of AXS/AM are expected to extend to important industrial sectors, particularly for military ballistic armor, where the feasibility for products with improved properties is critical. The use of AM offers a viable solution to overcome the difficulties associated with the conventional manufacturing methods, and thus offers greater design flexibility, cost efficiency, and reduced material waste. This review paper aims to contribute to the understanding of the current state-of-the-art and future research prospects for the production and applications of AXS/AM.

**Keywords:** honeycomb; sandwich panel; auxetic structures; auxetic materials; additive manufacturing; high-velocity impact; ballistic armor; anti-blast application

## 1. Introduction

Owing to the continuous and pressing need for lighter and stronger structures for space systems, aircraft and military equipment, the development of a novel easy to fabricate and cost-effective sandwich panel composite stands as the most appropriated structural material. Indeed, the sandwich panel is one type belonging to the main class division of "Structural Composites" designed to be lightweight with high stiffness and strength [1], as well as remarkable energy absorption characteristics under the impact from blast or projectiles [2].

A sandwich panel is composed of two outer plates' face sheets bonded by adhesive to an inner core as schematically illustrated in Figure 1. The outer plate in this figure must be made of materials strongly sufficient to resist the expected applied load in order to protect the inner core. According to Callister and Rethwisch [1], the core presents several functions: (i) provide support for the outer plates; (ii) hold them together with the adhesive contribution; (iii) have sufficient strength to withstand shear stresses; and (iv) be thick enough to resist buckling imposed by bending forces to the panel.



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**Figure 1.** Schematic of basic sandwich panel configuration. Reprinted with permission from [3]. Copyright 2012, MDPI AG.

The typical honeycomb structure for sandwich panels is fabricated with relatively thin foils arranged into interlocking cells exhibiting a proper configuration, which can display different geometrical patterns [4,5]. A characteristic hexagonal configuration exhibited in Figure 1 was the first proposed [6] and assisted as a basic model for other bio-inspired patterns [7,8], as depicted in Figure 2.



**Figure 2.** Horse-shaped honeycombs with different cross sections. Adapted with permission from Ref. [7]. Copyright 2018, Elsevier.

It is important to emphasize that these honeycomb structures were also investigated for their energy absorption applications [9,10], which might be a fundamental aspect for the presently reviewed ballistic application. In particular, auxetic structures (AXSs) possessing honeycomb patterns are being investigated as sandwich panels' cores for intrinsically higher energy absorption performance. As discussed in a prominent article, Yan et al. [11] indicated that this higher energy absorption of AXSs might be associated with both lowvelocity [12–15] and high-velocity impact caused either by the blast shockwave from bomb explosions [16–18] or by ballistic projectiles [19,20]. This latter will be included in the present review regarding complementary aspects to the work of Yan et al. [11].

In spite of comparative improvement in the physical properties of sandwich panels with an AXS core, owing to their negative Poisson's ratio (NPR), inherent fabrication difficulties and consequently higher costs were, until recently, a practical challenge for their common-scale engineering applications. The very recent remarkable review on anti-blast and impact performance of AXSs by Bohara et al. [21] discussed different manufacturing techniques and, in principle, recommended additive manufacturing (AM), also known as 3D printing, as it is currently the most used for small-scale pieces by enabling the construction of any kind of complex cellular structure such as those demonstrated in Figure 2. Furthermore, these authors indicate that future improvement in AM technology is necessary to produce large-scale AXSs for armor sandwich panels protecting personnel and vehicles from blast and impact projectiles.

Based on the aforementioned preliminary information, the objective of this article is to review the actual development and expected applications of 3D printing-processed AXSs intended for high-velocity impact protection as core sandwich panels. First, a deep discussion of relevant papers on AXSs, especially those not yet reviewed, is presented. Second, the current status of using the diversity of AM techniques for the fabrication of AXSs is critically discussed. Third, novel papers investigating the ballistic performance of 3D-printed AXSs are summarized. The following section discloses the existing and proposed ballistic and anti-blast applications for AXS. Final remarks on possible directions for large-scale production of AXSs, concerning specific interest as a material for ballistic armor, will provide the reader with an ongoing trajectory of a subject with indisputable future interest.

## 2. Properties of Auxetic Materiais

A novel class of materials, commonly known as "auxetics", possess peculiar structures that give them distinctive deformation characteristics [22]. In fact, materials deform in different ways when forces act upon them. The vast majority behaves in a traditional manner, in which an object expands axially under tension stress while contracting in the transverse direction, as illustrated in Figure 3a. The inverse ratio of transverse strain to axial strain, indicating a measure of how a material deforms under load, is known as the Poisson's ratio [23]. A material that stretches axially but contracts transversely in response to a tensile force, or enlarges transversely while axially contracting under compressive force has a positive Poisson's coefficient. The material owning auxetic behavior expands in the axial direction in one or more orthogonal directions under tension, exhibiting a negative Poisson's ratio (NPR), Figure 3b [24]. Under compressive forces, AXSs contract in both the axial and transverse directions, Figure 3d.

In the late 1800s, some discoveries about AXSs were made; however, they were not significant at that time. In 1882, the existence of AXSs cellular structures in iron mineral pyrite was reported, verified by torsion and flexural tests [25,26]. In 1893, Voigt [27] documented the auxetic effect and negative Poisson's coefficient in some materials. Until then, already known AXSs were limited to natural materials only, such as wood, and did not draw much attention to synthetic materials research. In 1987, almost a century later, Lakes [22] described for the first time an auxetic foam structure made of polyurethane (PU) that could be easily manufactured by compression and heating processes and that had an NPR equal to -0.6. Other works reported the existence of isolated materials possessing an NPR, such as bismuth, antimony and arsenic [28], cadmium [29],  $\alpha$ -cristobalite [30], as well as metals that crystallize in a cubic structure [31]. Some research has also demonstrated the existence of skin-like biological materials that exhibit auxetic behavior, such as cat skin [32], ox skin [33], and salamander skin [34], as well as human bones [35]. However, Lakes' study [22] assisted as a basis for future research on AXSs acquired synthetically.





**Figure 3.** Comparison of the mechanical behavior of conventional and auxetic materials under tensile and compressive forces: (**a**) Tensile forces acting on a conventional material; (**b**) Tensile forces acting on an auxetic material; (**c**) Compressive forces acting on a conventional material; (**d**) Compressive forces acting on an auxetic material.

After this discovery, research on AXSs has been developed for several sectors. The range of applications for these materials is quite wide, for example: sports artifacts [36,37], auxetic foams [38–40] and military use [41–43], biomedicine [44–47], textiles [48–50], etc. Auxetic materials are found in basically all known material classes: metals [51–53], crystals [54–56], polymers [57–59], ceramics [60–62], and composites [63–65]. Table 1 presents a brief list based on the most recent known AXSs and their respective NPRs.

Table 1. AXSs previously investigated and their Poisson ratios.

(a)

**Tensile Force** 

Material	Poisson's Ratio	Year	Reference
AA1060 aluminum	$-0.82 \sim -1.01$	2023	[66]
Cellulose	-0.2	2023	[67]
Carbon Fiber/Aluminum	-0.13	2023	[68]
LDPE	$-1.5 \sim -3.5$	2022	[69]
ABS	$-0.65 \sim -1.56$	2022	[70]
316L stainless steel	$-0.4 \sim -0.8$	2022	[71]
Graphene/Cu	$-0.19 \sim -0.25$	2022	[72]
Ba <sub>0.85</sub> Ca <sub>0.15</sub> Zr <sub>0.1</sub> Ti <sub>0.9</sub> O <sub>3</sub>	$-1 \sim -2$	2022	[73]
Cement/PU	$-0.21 \sim -0.47$	2022	[74]
PLA	$-0.50 \sim -0.78$	2022	[75]
MgHfN <sub>2</sub> and MgZrN <sub>2</sub>	-0.2	2022	[76]
PU/PDA/Graphene	-2.36	2022	[77]

AXSs diverges from conventional materials (CMs), presenting a peculiar behavior associated with unique mechanical properties. When experimentally investigated, AXS materials display superior properties reported as uncommon, when compared to CMs. An unusual deformation pattern under compression and tension is found for AXSs bringing forth many desirable properties, such as superior shear resistance [78], indentation resistance [79,80], fracture toughness [81], synclastic behavior [22], variable permeability [82] and improved energy absorption performance [83–85]. These properties are listed in the following subsections.

#### 2.1. Resistance to Indentation

The indentation resistance property occurs when a non-AXS is subjected to indentation, e.g., hardness testing. The load applied at the indentation location naturally compresses the material. To compensate for this localized pressure, it spreads perpendicular to the applied load, as shown in Figure 4a [86]. On the other hand, the AXSs behavior is different; when an indentation occurs on it, a local shrinkage is observed. Instead of spreading it perpendicularly, a flow occurs and accumulates under the indented region. Then, a denser area with higher indentation resistance is created below the indented zone, as depicted by Figure 4b [87]. As such, they have a higher resistance to indentation, when compared to CMs [79,88].



**Figure 4.** Deformation behavior and indentation resistance of: (**a**) conventional material and (**b**) auxetic material. Reprinted with permission from Ref. [89]. Copyright 2021, IOP.

The increased indentation resistance can be explained by the theory of elasticity. The indentation resistance is associated with the hardness of the material ( $H\alpha$ ) [90]. This property is correlated with the Poisson's ratio (v) given by:

$$H\alpha = \left[\frac{E}{(1-v^2)}\right]^{\gamma} \tag{1}$$

where *E* is the Young's modulus, *v* is the Poisson's ratio of the base materials, and  $\gamma$  is the constant that assumes the value 1 or 2/3 in the case of uniform pressure distribution or Hertzian indentation, respectively.

Based on Equation (4), it can be seen that, for isotropic three-dimensional (3D) materials, when the Poisson's ratio decreases to extreme values, for instance near -1, their hardness tends to infinity. Since the upper limit of Poisson's ratio for 3D isotropic solids is 0.5, the observed values are substantially lower. By contrast, the upper limit of the Poisson's ratio for two-dimensional (2D) isotropic systems is 1. Materials with such positive Poisson's values can also have infinite hardness values [24,91,92].

## 2.2. Shear Resistance

As demonstrated for indentation resistance, AXSs are more resistant to shear forces than CMs [90]. The classical theory of elasticity for 3D isotropic solids shows that the elastic

behavior of a body can be described by two out of four constants: the Young's modulus (E), the shear modulus (G), the bulk modulus (K) and the Poisson's ratio (v) [93]. In 3D solids, the relationship between these constants is given by the following equations [88]:

$$G = \frac{3K(1-2v)}{2 \cdot (1+v)}$$
(2)

$$G = \frac{E}{2 \cdot (1+v)} \tag{3}$$

From these equations, it is inferred that the value of shear modulus increases as a function of the reduction in the Poisson's ratio, resulting in a shear strength increase. The range of elastic modulus corresponding to instability and stability under different conditions is shown in the map of Figure 5. It indicates that the Poisson's ratio of the isotropic solid should be ranging from -1 to 0.5. When it approaches -1, the shear modulus tends to infinity.



**Figure 5.** Map showing the elastic material properties corresponding to different values of K-modulus and shear modulus G. Reprinted with permission from Ref. [94]. Copyright 2007, Wiley.

# 2.3. Fracture Resistance

AXSs display better fracture resistance than CMs [81]. AXSs also exhibit low crack propagation, requiring a greater amount of energy to expand than CMs [95]. Thus, auxetic materials present brittle fracture. Some works concerning the fracture toughness behavior of AXSs are worth reviewing. Maiti et al. [96] demonstrated that the stress intensity factor ( $K^*_{IC}$ ) for conventional foams is proportional to the normalized density and can be described by:

$$\frac{K_{\rm IC}^*}{\sigma_{\rm f}\sqrt{\pi l}} = 0.19 \cdot \left(\frac{\rho_*}{\rho_{\rm s}}\right) \tag{4}$$

where  $\sigma_f$  is the fracture stress of the cell rib, l is the rib length,  $\rho^*$  is the foam density, and  $\rho_s$  is the density of the foam based material.

Some works reported increased fracture toughness of AXSs, while CMs did not disclose the same behavior. Yang et al. [97] have produced epoxy/Kevlar auxetic laminate composites and correlated the mechanical properties with plain Kevlar and polyurethane (PU)

treated Kevlar fabrics. From the fracture initiation toughness ( $G_{IC}$ ) test, the authors observed that the auxetic fabrics disclose superior performance as compared to plain and PU treated kevlar fabrics, as illustrated in Figure 6. Some conditions of the auxetic epoxy/Kevlar composite disclosed a  $G_{IC}$  value up to 225% higher than untreated woven Kevlar and up to 125% higher than PU-treated Kevlar.



**Figure 6.** Fracture initiation toughness (G<sub>IC</sub>) for all types of composites. Reprinted with permission from Ref. [97]. Copyright 2017, Elsevier.

#### 2.4. Energy Absorption

AXSs manifest superior properties regarding energy absorption. Ultrasonic, acoustic and damping energy absorption are characteristics in which AXSs have an advantage over CMs. It is reported that auxetic foams can display better sound absorption ability than conventional foams at low frequencies [83]. Dynamic crushing properties were remarkable in the auxetic foam, while the conventional foam did not show significant resilience at a high constant stress rate [98].

Oh et al. [99] developed an auxetic foam made of PU and filled with wrinkled 2D graphene oxide (GO). The authors investigated the properties of acoustic energy absorption and damping absorption. Auxetic foam reinforced with GO was set side by side with another AXS without filling. Graphene-polyurethane oxide auxetic foam exhibited high sound absorption performance, with a range of 98.4% at 2 kHz due to the hierarchically porous structure. The improved mechanical compression stability is attributed to the superior energy absorption properties resulting from superb compressibility and internal auxeticity. This greatly increases the shock energy absorption time by 189% in the low-velocity impact test in contrast to the value of the pure PU foam. The blending of a 2D corrugated GO sheet and a flexible 3D AXS promoted greater acoustic and vibration absorption as a consequence of multiple energy dissipation mechanisms.

Najafi et al. [100] analyzed the mechanical performance and energy absorption in order to show differences and likenesses of three different AXSs produced in ABS by the 3D printing method: re-entrant, arrowhead and anti-tetra chiral, as depicted in Figure 7a–c. From the compression test results, the authors observed that the anti-tetra chiral structure presented a greater deformation (Figure 7d–f), when set against the arrowhead and re-entrant structures. Nevertheless, this structure also brought up a significantly higher specific energy absorption (SEA), illustrated in Figure 7g.





## 2.5. Synclastic Behavior

Synclastic behavior is the ability of an AXS to suffer deformation into a dome shaped curvature when subjected to bending stresses [101]. Contrastingly, CMs uncover a stretching saddle-shaped on their surface when subjected to bending stresses, originating a shrinkage in their perpendicular direction. Therefore, it presents an anticlastic curvature, as shown in Figure 8a. On the other hand, the AXs, when bent, will present a dome shape because, throughout the application of stress, there is an expansion and contraction of the material both on the outside and inside, respectively [102]. Thus, the result of the expansion of the tensioned part and the shrinkage of the compressed part is the dome shape, shown in Figure 8b. This property is desired in materials for application in the biomedical and sports sectors, such as stents, prostheses, sports accessories, etc. [23,36,37,103–106].



**Figure 8.** Curvature in bending: (a) anticlastic curvature of conventional, non-auxetic materials and (b) synclastic curvature of auxetic materials. Reprinted with permission from Ref. [37]. Copyright 2018, MDPI AG.

## 2.6. Variable Permeability

Currently, it is already known that AXSs own a porous microstructure and that its dimensions can vary under tensile or compressive stresses. Given this characteristic, a potential use that emerges from AXS porosity is the application in filters. Alderson et al. [107] detailed in their work that AXSs may offer superior performance in filter application at both the macro and nano-scale in view of their unique pore opening properties and characteristics. Variable permeability is paramount for medical applications such as smart stents, which are used to deliver pharmaceutical drugs into the human body [108,109]. In Figure 9, a schematic view of how variable permeability works is illustrated, in which a stress applied to the AXS develops the expansion of the pore structure, allowing a particle to go across it.



**Figure 9.** Schematic of variable permeability in auxetic structures. Reprinted with permission from Ref. [110]. Copyright 2020, Wiley.

# 2.7. Shape Memory Auxetics

Another important property related to AXSs is shape memory. It occurs when a material subjected to deformation, whether plastic or elastic, has the ability to return to its original state after undergoing thermal excitation [111,112]. Currently, there are several studies reporting the shape memory effects in materials of different classes—for instance, NiTi alloy [113–115], PLA/TPU/Fe<sub>3</sub>O<sub>4</sub> [116], SMEP/GNP [117], ZrO<sub>2</sub>/Y<sub>2</sub>O<sub>3</sub> shape memory ceramic [118], among several others performing this singular characteristic. Studies demonstrate that it is possible to obtain auxetic foams that can be reverted to conventional foams several times without a loss of mechanical properties [119]. Therefore, shape memory is useful in situations that require variable auxetic and non-auxetic mechanical properties, being changed as a function for the temperature.

In Figure 10, a schematic of this effect in an AXS developed by Kamyab et al. [120] is illustrated for an acrylate shape memory polymer (SMP). In the schematic, it is possible to observe that, with the heating of the material, tensile stresses start to act, as a consequence. After this process, the SMP is cooled, and then its load is removed, inducing it to return to its first state. Finally, it is reheated in order to completely return to its original state.



**Figure 10.** Schematic illustrating the thermo-mechanical loading cycle under tensile mode for shape memory polymer (SMP). Reprinted with permission from Ref. [120]. Copyright 2022, ProQuest.

## 2.8. AXSs for Ballistic Protection

In Section 2, the properties of auxetic panels were described, which are made possible by the complex structures that compose them. In Section 3, these structures will be presented in more detail. The development of auxetic panels with these structures allows for the absorption of impact energy, which can be applied in various areas, such as protection of military vehicles against explosions and ballistic panels. According to Bohara et al. [21], energy absorption occurs in AXSs due to the deformation of the cell wall and the subsequent formation of plastic hinges in the wall. The inherent porosity of AXSs also contributes to greater energy absorption. The authors cite studies that show the use of AXSs in blast armor, vehicle bumpers, impact shields, and protective helmets.

An interesting example is the study by Yan et al. [11], who evaluated AXS honeycomb sandwich panels impacted by projectiles, made with carbon fiber-reinforced polymer. Figure 11 schematically illustrates the penetration of the bullet into the AXS. The authors observed that, as the bullet perforates the front steel plate, the honeycomb cells in its path are directly cut, resulting in brittle failure and delamination. The external steel plate had little effect on reducing the bullet's velocity but contributed to reducing the crushing area. On the other hand, the internal core of the honeycomb played an important role in reducing the penetration velocity and, consequently, the impact energy.



**Figure 11.** The perforation process of bullet penetration into AXS honeycomb sandwich plate. Reprinted with permission from Ref. [11]. Copyright 2022, Elsevier.

#### 3. Auxetic Structures

The term auxetic is used for both structures and materials. The AXS plays a key role in this material expansion and mechanical behavior. Therefore, several structural models have been investigated, and their auxetic behaviors have been discussed. For this topic, the main models of auxetic-related structures will be described.

#### 3.1. Re-Entrant Structures

The re-entrant pattern is one of the most well-known structures used for developing AXSs. It was originally proposed in 1982 by Gibson et al. [121], where, from the deformation of a hexagonal honeycomb structure, it was possible to obtain 2D re-entrant structures, as schematically shown in Figure 12. When a load is applied, the diagonal ribs are stretched, moving the structure and giving rise to the auxetic effect.



**Figure 12.** Auxetic behavior of the re-entrant structures. Reprinted with permission from Ref. [122]. Copyright 2022, Wiley.

As a result of the development of this structure, advances in the development of AXSs have been significant. From the original re-entrant structure, others have been proposed, as illustrated in Figure 13. Similar to the re-entrant structure, the arrowhead and star models (Figure 13b,c) have the auxetic behavior coming from the re-entrant parts, as highlighted by the blue color in the figure. Using rhombus-shaped lines, the hexagonal re-entrant and grid-like models were established (Figure 13d,e). In Figure 13f, a sinusoidal structure is illustrated, in which one can observe the elongation occurring and, for this reason, the

auxetic effect arises. In addition, links on the sinusoidal curves can be modified following the articulated linear ligaments.



Figure 13. Re-entrant structures. (a) re-entrant honeycomb; (b) double arrowhead; (c) star honeycomb; (d) structurally hexagonal re-entrant honeycomb; (e) lozenge grids; (f) sinusoidal ligaments. Reprinted with permission from Ref. [104]. Copyright 2021, MDPI.

# 3.2. Rotating Unit Structures

Another type of AXSs is related to rotating unit structures. In this model, different uniform geometric shapes such as rigid/semi-rigid squares, triangles, rectangles and tetrahedra are configured at their vertices [123–125]. The auxetic behavior of this structure occurs through the rotation of these shapes when stretched in a certain direction. This model was firstly proposed by Grima et al. [126], when they verified the occurrence of AXS in an inorganic material. The concept of rotating squares with rigid units was shown to be independent of the initial geometry and the direction of loading applied to the material, keeping the NPR near -1 [127]. Several studies have been conducted in order to better understand the deformational characteristics of this AXS.

The square rotating unit, Figure 14a, is the simplest 2D structure among a variety of 2D unit structures available to be manufactured. It is possible to acquire rectangle or parallelogram units by scaling and tilting square structures, as presented in Figure 14b [128,129]. It is also possible to acquire a rotating unit with two or more different types. Typical examples of these heterogeneous rotating units are the trans-rectangular, Figure 14c, and the two-square structures, Figure 14d. In addition, for rotating frames possessing a square section, there are 2D rotating frames with triangular units, owning three hinge points. They were manufactured similarly to the square type, but their structure is simpler, and might be developed based on simple geometrical units such as triangles, as shown in Figure 14e–g. The rotating structure that has a hexagonal unit, Figure 14h, can be used in two ways: (i) the hexagon attached to a square or triangular unit or (ii) triangular unit. However, it cannot be used individually to manufacture a rotating structure, without square or rectangular units. A hexagonal is employed with other types of units to create a heterogeneous rotating 2D structure.



**Figure 14.** AXSs Rotating units: (**a**) square; (**b**) rectangular; (**c**) trans-rectangular; (**d**) bisquare; (**e**) triangular; (**f**) isosceles triangular; (**g**) bi-triangular; and (**h**) hexa-triangular.

# 3.3. Chiral Structures

Chiral structures are manufactured by straight ligament connections (ribs) joined to central nodes that can be circles or other geometric shapes. The auxetic behavior regarding this structure is achieved by wrapping or unwrapping the ligaments around the nodes when a load is applied.

The unit circles present in chiral structures are uniformly aligned in tri-, tetra-, or hexahedral arrangements, where the ribs wrap around the circles and connect them to others. When a load is applied to a chiral structure, it is transferred to the circular units via chiral ribs, and the transmitted load is deflected from the center of the circle, producing a rotational torque. Thus, it rotates in a particular direction pulling and pushing adjacent units amongst ribs connected in a different direction of the load [130]. Two-dimensional chiral structures are composed of circular units and ribs, and are limited to five different basic types: tetrachiral, anti-tetrachiral, trichiral, anti-trichiral, and hexachiral, as illustrated in Figure 15 [131].

Chiral structures are produced from narrow designs, which have similar auxetic characteristics to re-entrant structures. Even though the high porosity of chiral structures allows them to be lighter than re-entrant models, this reduction in weight ultimately obstructs the durability and stability. Moreover, even if the chiral structure exhibits NPR, it becomes vulnerable to local buckling if compressive loads between circular units are transmitted through thin ribs. Furthermore, due to the geometric arrangement, they have limited structural variation and narrow design space, unlike the re-entrant and rotating structures.



**Figure 15.** Chiral AXSs: (**a**) tetrachiral; (**b**) anti-tetrachiral; (**c**) trichiral; (**d**) anti-trichiral; and (**e**) hexachiral structures.

# 3.4. Nodule and Fibril Structures

Nodule and fibril structures consist of a rigid unit connected among fibrils. These fibrils are responsible for the load transfer to the rigid structures. The working scheme is schematically illustrated in Figure 16; without a load acting upon them, they are twisted around the rigid unit. When a tensile force is applied to the fibril structure, they tend to align and push it in a perpendicular direction, inducing an auxetic behavior. Initially, Alderson and Evans [132] developed a model for a polymer featuring auxetic micropores. These AXSs can be subdivided into classes based on how the rigid units and fibrils are connected: (i) network type; with (ii) circular or (iii) square nodules; and (iv) bundle type [133].



(a) Before Compression

(b) After Compression

Figure 16. Typical shape of fibril-nodule structures: (a) before compression; (b) after compression.

The fibril–nodule model was developed early in studies concerning AXSs, to be employed in polymeric materials. An example of an auxetic polymer is the liquid crystalline, where its behavior can be defined by the fibril–nodule mechanism. This material has a crystalline fibril–nodule structure when it has no load acting upon the material. However, when a stress is applied, it presents an amorphous AXS due to the decrystallization with its stretching [134]. Given this concept, the auxeticity of the fibril–nodule structures only occurs for a tensile condition, disappearing under the action of compressive loads.

## 3.5. Interlocking Structure

The auxetic interlocking structure was first proposed by Ravirala et al. [135], and its associated micromechanical model is schematically illustrated in Figure 17. The structure without a stress state is all connected and interlocked, Figure 17a. At the moment, a load is applied, it expands, exhibiting auxetic behavior, Figure 17b. The conventional hexagonal geometry shown in this model ( $0 < \alpha < 90$ ) displays an auxetic behavior regarding its structure, while the reentrant hexagons ( $90 < \alpha < 180$ ) disclose a positive Poisson's coefficient.



Figure 17. Interlocking hexagon structure: (a) fully densified; (b) partially expanded.

#### 3.6. Keyed Brick Structure

The keyed brick structure is designed to withstand the horizontal components of the forces generated throughout an earthquake, while allowing a motion that assists with differential thermal movements between the graphite core and the steel supporting the edges [86]. The free movement of the core was also designed to sustain the expansion and shrinkage of the graphite bricks when radiation exposure occurs. Furthermore, the structure needs to have high shear deformation resistance in the horizontal plane and low resistance to volume changes. As such, it expands in all radial directions when subjected to a tensile load in the horizontal plane and keeps the square mesh over deformation. In this way, this type of model becomes auxetic, obtaining  $v = \pm 1$  in the horizontal plane [86]. They are arranged in columns of  $10 \pm 12$  bricks, making the entire core possible to be approximated to a continuous anisotropic solid material. The scheme of the keyed brick structure is illustrated in Figure 18.



Figure 18. Schematic of a keyed brick structure.

## 3.7. Other Geometries

In addition to the most well-known AXSs that were presented in the previous items, there are several other cellular structures that present auxetic characteristics. These structures end up forming new classifications, and it is often not possible to classify them according to the models already known.

Bohara et al. [85] developed three new AXSs for application in military vehicles protection by absorbing blast energy. They were named: (i) hourglass structure (HGS); (ii) braced cross-petal structure (BCPS); and (iii) cross-petal structure (CPS). The finite element method (FEM) was employed to analyze these novel ASXs using a variety of parameters such as stress–strain behavior, Poisson's ratio, energy absorption capacity and others. From the simulations, the authors found that, for demands requiring high energy absorption, these three AXSs have shown superior performance contrasting the traditional ones. Figure 19 depicts a comparison of the specific energy absorbed (SEA) for all AXSs analyzed.



**Figure 19.** SEA values for different AXSs. Reprinted with permission from Ref. [85]. Copyright 2021, Elsevier.

Moreover, another approach for acquiring novel structures is the union of two AXSs. Etemadi et al. [136] developed hybrid structures attaching re-entrants and arrowhead structures (RAH), Figure 20a, as well as star and arrowhead structures (SAH), Figure 20b. The authors produced the samples by the 3D fused deposition method using a standard polylatic acid (PLA) resin for the manufacture. FEM analyses were performed, as well as tensile and compression tests, in order to evaluate their mechanical properties. From the analyses, it was found that the hybrid models have shown higher E and *v* than re-entrant and arrowhead ones. RAH and SAH achieved E and *v* values of 66.21 and 86.24 GPa, and -1.34 and -0.98, respectively. On the other hand, the re-entrant and arrowhead conventional structures presented the following values: E = 22.86 and 34.67 GPa and v = -1.24 and -1.00, respectively.



**Figure 20.** Hybrid structures: (a) re-entrant arrowhead (RAH); (b) star arrowhead (SAH). The reentrant, star, and arrowhead structures are illustrated in colors for better understanding. Reprinted with permission from Ref. [136]. Copyright 2023, Elsevier.

#### 3.8. Brief Summary

In this section, it is worth noticing the impressive number of distinct models of auxetic structures that have been investigated so far, from reentrant [121,136] to cross-petals [85] for absorbing blast energy. It predicts a vast field of opportunity for the development of novel auxetic structures.

## 4. Manufacturing Techniques of Auxetic Structures

The special properties obtained through the development of AXSs are associated with their origin in the manufacturing of a complex 3D structure. Additionally, small details such as the reentrance dimensions of a unit cell are crucial to this auxetic behavior. However, these details also make it difficult to fabricate these materials using conventional techniques. To overcome this challenge, additive manufacturing (AM) techniques are employed in the fabrication of these structures. AM provides a quick and precise solution in the manufacturing of AXSs sandwich panels that present complex geometries at their core. However, conventional techniques are also used, albeit less commonly, in the fabrication of AXSs [137]. Currently, there are several manufacturing techniques available for the production of AXSs, including both conventional and AM/3D printing techniques such as:

- Self-Propagating Photopolymer Waveguide (SPPW);
- Microstereolitography (µSLA);
- Direct Laser Writing (DLW);
- Self-Assembly
- Selective Laser Melting (SLM).

#### 4.1. Self-Propagating Photopolymer Waveguides (SPPW)

The self-propagating photopolymer waveguides (SPPW) technique assembles a 3D polymeric structure in a cellular microscale arrangement, interconnected periodically [138]. It consists of an ultraviolet (UV) light beam enlightening a 2D mask, which has an aperture

inside a photomonomer container, as demonstrated in Figure 21 [139]. The SPPW is based on the incident light self-trapping effect upon the polymer, being induced by a change in the refraction index among the liquid monomers and the rigid polymeric material. Owing to this event, the SPPW is able to create high aspect ratio beams having a continuous crosssection, being perfect for the 3D topologies construction based on beams. Furthermore, it is possible to control the topologies by an aperture pattern on the mask and orientation of the incident UV light. While the unit cell dimension and the smaller size details, regarding the topologies, rely on the aperture diameter and mask space. The material thickness is controlled mostly by the maximum waveguide length propagation. Moreover, a multilayer strategy could be applied in order to acquire structures displaying a higher thickness [140].



**Figure 21.** Operational scheme of the self-propagating polymer waveguide (SPPW) technique. Reprinted with permission from Ref. [138]. Copyright 2007, Wiley.

However, in contrast to other AM techniques, the SPPW is limited regarding the topologies randomness, since it is just possible to manufacture variations of beam-based topologies. The extended UV light exposure requested to achieve the maximum waveguide length often enlarges the original diameter, developing thicker materials [138]. On the other hand, the great advantage of it is the high manufacture speed, being able to produce microscale AXS in a few minutes in addition to a great scalability capacity, yielding manufacture rates superior to  $1 \text{ m}^2/\text{min}$  [141]. The aforementioned characteristics make it an attractive method for large-scale fabrication.

### 4.2. Microstereolithography (µSLA)

Microstereolithography ( $\mu$ SLA) is an AM technique classified according to the ISO/ASTM 52900:2021 standard [142] as belonging to the Vat Photopolymerization (VPP) category.  $\mu$ SLA uses a UV light beam to cure the resin, resulting in the rapid assembly of structures. The operational mechanism of the SLA technique is based on the local polymerization of a photosensitive resin, as shown in Figure 22. Each layer is obtained by moving the UV light beam over a surface, which is guided on the *x*- and *y*-axes by galvanometric mirrors. The solidified object is then immersed in a resin reservoir, and a new layer is reflected onto the already polymerized layer, allowing the manufacture of the next layer [137,143,144].



**Figure 22.** Schematic of microstereolithography technique. Reprinted with permission from Ref. [145]. Copyright 2020, Elsevier.

Furthermore, the AM techniques yielded a strong influence on the production of industrial parts because they significantly reduced the processing time, entailing a manufacturing economy regarding objects with complex geometry. The  $\mu$ SLA was one of the first to be developed, and due to its velocity, is, hitherto, the most applied in industry. The manufacturing costs for the  $\mu$ SLA pieces are affordable, and the surface finishing is appropriate, without a requirement for further operations. The typical resolution range for  $\mu$ SLA is 150 mm for the three space directions. However, some parameters, such as: resolution, precision, and surface roughness may change since they are based on over layering. In particular, the vertical resolution (over the construction axis) is associated with the overlapped layer thickness, whereas the lateral resolution (on the plane) is determined by the light beam dimension used to design each layer shape on the resin surface.

In comparison to others' AM, the paramount  $\mu$ SLA advantage is the production of 3D microscale objects holding complex structures and supporting a high velocity fabrication. On account of these compelling characteristics,  $\mu$ SLA is assigned to several fields such as: biomedicine, tissue engineering, micro-optic devices, bioinspired materials, micro-electromechanical, among other systems [146–149].

The  $\mu$ SLA is relevant regarding the development of AXSs since it can produce with ease auxetic cores for sandwich panels, and therefore apply them on a large scale. Alomarah et al. [150] manufactured re-entrant AXSs and re-entrant chiral auxetic (RCA) composed of a photopolymer composed by polypropylene (PP) by  $\mu$ SLA. In a more recent work, Varas et al. [151] also used PP to produce different types of AXSs and evaluate the properties of each structure.

## 4.3. Direct Laser Writing (DLW)

Direct laser writing (DLW) is a well-known AM method for the fabrication of complex structures on a nanoscale up to 100 nm [152]. In this method, a beam laser is focused through an objective lens in order to cure photopolymers by means of a single or multi-photon absorption [153,154]. The DLW by single-photon absorption is limited to the manufacture of 2D structures because its absorption occurs inside a whole area of photopolymers exposed

to light. The multi-photon absorption, also known as two-photon polymerization, takes place in a small voxel on the focal point of the laser beam, where the light intensity is remarkably high [155]; thus, arbitrary 3D structures possessing details excessively smaller could be fabricated by the voxel [156,157]. As a consequence, this process is an attractive tool for applications in several fields, such as micro-optics, supercapacitors, microfluidics, biomedical implants and tissue engineering [158–164]. In Figure 23, the schematic diagram of how the DLW works is illustrated.



**Figure 23.** Setup of the direct laser writing system. Reprinted with permission from Ref. [153]. Copyright 2020, ACS.

The principle of the DLW is based on a laser beam that is pulsed at a wavelength close to infrared ( $\lambda$  = 780 nm). This laser is focused on a photoresist material, transparent to the wavelength, through a high aperture objective lens. The photoresist contains photoinitiators for the absorption of two-photons. Due to the focus through the objective lens, the photons are absorbed within the focal volume. Thus, initiators cause a chemical reaction when excited, which enables the formation of chemical bonds, for example, by polymerization or bond breaking. During sample manufacturing, moving the focal spot in different directions enables the fabrication of complex 3D structures at high fabrication speeds [165].

The DLW is able to manufacture materials without the necessity of supporting matrices or a layer by layer process, as the SPPW, owing to the capacity to precisely induce the polymerization within a particular spatial position of a photoresist thick-film [166]. Despite the aforementioned benefits, the DLW is not widely applied for mass production in all industries because it is much less scalable than other methods. Additionally, the costs of acquiring and conserving DLW systems are very high because accessories such as optical systems and femtosecond lasers are expensive and difficult to obtain. Thus, the process becomes unfeasible for large-scale fabrication of AXSs. Another factor that makes this technique inaccessible in the production of AXSs is the choice of photoresist materials. Because the transparency to the infrared beam is necessary for the processing to occur, and the selection of materials is limited to transparent polymers, other materials such as metallic and ceramic particles are not attainable in the process because they inhibit the penetration of the laser.

# 4.4. Self-Assembly

The Self-Assembly technique is characterized by the mechanism of polymeric phase separation, which can be in the form of emulsion or colloidal suspension. Although

previously not considered an AM technique, due to its technological unfeasibility for such classification, since 2018, research involving this manufacturing method has been growing exponentially, allowing the technique to gain technological maturity to be classified as an AM technique [167]. This is due to its ability to rapidly produce complex structures in a distributed manner, making it a method of great importance during the COVID-19 pandemic between 2020 and 2022 [168–170]. The interactions between the components in the fabrication present van der Waals bonds, hydrogen bonding, electrostatic attraction, as well as hydrophobic and hydrophilic interactions. These interactions can create a self-assembly system owing to a thermodynamic condition of non-equilibrium, establishing a stable state within well arranged hydrophobic structures [171–173]. It is possible to develop materials with organized nanostructures from the separation of the microphases present in the material. Self-assembly is very competitive when compared to other AM techniques owing to the ability to produce parts with customizable morphology and functionalities [137].

In order to manufacture materials on a large scale, a block copolymer (BCP) phase separation technique was developed. BCPs are divided by the management of chemical properties and molecular weight of each polymer. The self-assembly by BCP separation occurs by the thermodynamic incompatibility of the copolymer phases, where a separation of microphases with a variety of nanoscale morphologies is generated, such as: lamellas, spheres, cylinders and others [174–176]. In Figure 24, a schematic of the separation and arrangement of the BCPs microphases is illustrated.



**Figure 24.** Schematic of self-assembly. The AM method uses a substrate template to give long-range order to lamellar and cylindrical self-assembled block copolymer films. Reprinted with permission from Ref. [177]. Copyright 2016, Nature.

Manufacturing nanostructured materials by self-assembly is not limited only to polymers. Metallic and ceramic structures can also be processed by this technique; for instance, it has already been developed nanostructures of gold [178],  $CeO_2/MnO_x@C$  [179] CoPC/CNTs [180],  $Fe_3O_4/rGO$  [181] among others for several applications.

In comparison to other AM, self-assembly yields a unique low-cost opportunity, highly scalable and a fast manufacture for 3D structures possessing micro and nanoscale. However, this process's ability for the fabrication of several morphologies, such as octet or cubic plate lattices, is still very limited. In addition, up to now, it is difficult to manage a self-assembled final topology [173]. As a consequence, defects are acquired in large-scale fabrications, and further investigations are required to solve these problems.

# 4.5. Selective Laser Melting (SLM)

The selective laser (SLM) is another method for the construction of 3D metallic structures. It uses computational support and a high energy laser in order to bond the metallic particles [182]. SLM makes viable the manufacture of metallic components layer by layer following a 3D-computer aided design (CAD) model. Thus, this enables an almost unlimited fabrication of complex geometries without the necessity for pre-production costs or specific tools [183]. The SLM mechanism is demonstrated in Figure 25, and occurs according to the following steps: (i) the 3D-CAD model is decomposed in layers and sent to a selective fusion laser equipment; (ii) a powder material is laid upon the substrate, creating a thin layer; (iii) each piece of geometry information is transferred by the laser beam to the powder bed where the regions having the solid materials are scanned under an inert atmosphere; thus, another layer can be manufactured; (iv) after a layer is constructed upon the substrate, the equipment bases connected to a plunger go down, so a new layer is inserted above the first one. Therefore, the manufacturing steps are repeated layer by layer until the sample is constructed [184,185]. The printed samples can reach a density value close to 100% because metallic powders are used, disclosing suitable mechanical properties combined with a rigorous management of the material composition [186].



**Figure 25.** Schematic of selective laser melting 3D printing method. Reprinted with permission from Ref. [187]. Copyright 2017, Elsevier.

The AXSs production by SLM allows the acquisition of materials with superior mechanical properties compared to the auxetic ones composed of polymers. A great majority of AM techniques process polymer structures. Although they present acceptable properties, they still exhibit limited characteristics, in comparison to metals in terms of a greater thermal and mechanical resistance. Singh et al. [188] processed re-entrant AXSs by SLM. They adjusted parameters and mechanical tests and were able to attain a Poisson's Ratio of -3.1. Gao et al. [189] brought on auxetic contacted cube (ACC) structures by SLM using an AlSi10Mg alloy. The authors observed a superior density to 99% for the specimens; in addition, they displayed NPR and a good deformation distribution for all the samples.

#### 4.6. Other Techniques

In addition to the previously mentioned techniques, there are several others for the production of AXSs. Each method has its own process particularities, making it viable to construct complex structures fast and with ease. As mentioned in the text, AXSs can be produced by both conventional techniques and more advanced techniques, such as AM techniques. Among all the available techniques, it is worth mentioning: extrusion [190–192], fused deposition modeling (FDM) [193–195], inkjet printing [196,197], selective electron

beam melting (SEBM) [198–201], selective laser sintering (SLS) [202–205], aerosol jet printing [206–208], chemical vapor deposition (CVD) [209–211], and others. Classifying these techniques is a complex task because the research areas for the AM and AXSs present an accelerated expansion. However, certain methods may show similar features but manufacture distinct materials classes. Therefore, it is not possible to classify them in order to expand a range of applications and materials.

#### 4.7. Brief Summary

In this section, the relevance of combining AXS and AM was emphasized. Indeed, the numerous proposed AXS, despite their complex shapes, certainly have a proper technique for cost-effective fabrication of armor protection against high-velocity projectile and blast protection.

#### 5. Applications

The sandwich panels having a core assembled by AXSs present remarkable properties, allowing them to be applied in a variety of distinctive applications, such as biomedical, textiles, sports and military. The AM techniques enable fast processing for materials holding complex structures, while they display great precision and replicability. For this reason, these materials become attractive for large-scale demands. Table 2 presents the main sector and applications for auxetic materials manufactured by AM methods.

Field	Application
Aerospace	Vanes for engine, thermal protection, aircraft nose-cones, wing panel, vibration absorber
Automotive	Bumper, cushion, thermal protection, sounds and vibration absorber parts, fastener
Biomedical	Bandage, wound pressure pad, dental floss, artificial blood vessel, artificial skin, drug-release unit, ligament anchors, surgical implants
Composite	Fiber reinforcement
Military	Helmet, bulletproof vest, knee pad, glove, protective gear
Sensors/Actuators	Hydrophone, piezoelectric devices
Textile	Fibers, functional fabric, color-change straps or fabrics, threads

Table 2. Summary of the main applications for auxetic materials [87,212].

Among the specified applications in Table 2, the area showing promising potential is in the military field. The AXSs are outstanding because they have the capacity to absorb high-velocity impacts, i.e., shock waves and blasts, commonly applied to bullet vests and ballistic helmets [213–215]. Moreover, auxetic materials enable the production of more lightweight and greater uniform shock wave energy absorption; thus, soldiers acquire higher mobility on the battlefield [36,216]. An example is a shoe based on an auxetic material, capable of reducing the body weight impact upon the ground, preventing injuries and providing more comfort [217].

High-speed military applications encompass ballistic protection, in which armor must absorb the energy of projectiles traveling at speeds above 300 m/s and prevent the dispensed projectile and/or shock wave from causing injury to the combatant. These speeds are classified in different ways according to the NIJ 0101.06 standard [218]. From these speeds, it is possible to classify light armor and heavy armor. Soft armor is classified in the lower and medium levels in the NIJ standard, IIA, II, and IIIA, in which protection requirements are against low-energy projectiles, such as the bullets shot from handguns [219,220]. The higher levels must include hard armor inserts in what is called "in conjunction design". Those plates are destined for high-risk military applications, since they are subjected to higher energy projectiles, such as the bullets from AK-47s. Table 3 indicates the relationship of impact velocities of different projectile types to armor levels according to NIJ 0101.06 [218].

Armor	Test	Bullet	Armor Test
Type	Bullets	Mass (g)	Velocity (m/s)
IIA	9 mm FMJ RN	8.0	373
	0.40 S & W FMJ RN	11.7	352
П	9 mm FMJ RN	8.0	398
	0.357 Magnum JSP	10.0	436
IIIA	0.357 SIG FMJ FN	8.1	448
	0.44 Magnum SJHP	15.6	436
III	7.62 mm NATO FMJ	9.6	847
IV	0.30 Calibre M2 AP	10.8	878

Table 3. Test requirements from NIJ 0101.06 standard [218].

Considering the application of AXSs in anti-blast and high-velocity (impact and ballistic), Table 4 shows a summary of the most recent research investigating the behavior of auxetic materials for military demands.

**Table 4.** Summary of recent papers discussing the auxetic sandwich panels for anti-blast and ballistic applications.

Author	Year	Material of AXS	Structure	Application
Liu et al. [221]	2023	Carbon Fiber/PU	Double-Arrow	Ballistic Protection
Jiang et al. [222]	2023	Aluminum AA6061/Grade 800 HSS	Re-entrant Circular (REC)	Blast Protection
Lan et al. [223]	2023	AlSi10Mg aluminum alloy/5052 aluminum alloy	Hybrid Chiral	Ballistic Protection
Haq et al. [224]	2023	Aluminum AA2024/Armor Steel	Re-Entrant/Hexagonal Star/Re-Entrant	Ballistic Protection
Yan et al. [225]	2022	AlSi10Mg aluminum alloy/Q345 steel	Hexagonal and Re-Entrant	Blast Protection
Critchley et al. [226]	2022	TPU	Re-entrant	Blast Protection
Usta et al. [227]	2022	CFRP/PLA	Re-entrant	Ballistic Protection
Wu et al. [64]	2022	Kevlar	Hexagonal and Re-entrant	Impact Resistance

A relevant observation regarding the works previously mentioned in Table 4 is that most of them present a re-entrant structure. From the economic perspective, it is simpler to be designed, consumes less material for its manufacture, and less processing time is required. However, other models are being investigated for ballistic and anti-blast applications, such as the double-arrow [221], re-entrant circular [222] and hybrid structures [223,224].

Liu et al. [221] have developed sandwich panels consisting of double-arrow AXS, aiming to ballistic demands. The researchers fabricated the sandwich structure by the prepreg method, using carbon fiber reinforced polymer (CFRP) as the material for the panels. The auxetic core was also made of CFRP and manufactured by the computer numerical control (CNC) method, attached to the panels employing an epoxy resin and hot pressing process. Subsequently, the auxetic cores were filled with PU foam. The residual velocity tests were performed with a projectile's incident velocity ranging from 75 to 178 m/s. The experiments were carried out by correlating the auxetic sandwich panel filled with PU and another specimen without the foam. From the ballistic test results, the authors discovered that, when the incident velocity was up to 105 m/s, the residual velocity for both panels conditions was the same. However, it was observed that the auxetic panel filled with PU foam presented a decrease in the residual velocity when there was an increase in the incident velocity. Thus, it shows a higher energy absorption throughout the ballistic impact.

Jiang et al. [222] published a study regarding the development of an auxetic sandwich panel for anti-blast protection that may be used in automobiles, ships, buildings and

others. The novel material was based on a re-entrant structure. The authors modified it and produced the re-entrant circular (REC) model. It consists of a circular reinforcement attached to each side of the cellular wall. The panels were manufactured using 800 HSS steel, and the auxetic core was fabricated with AA6061 aluminum alloy. Explosion tests were performed, allowing the investigation concerning the absorption power of this AXS. From the acquired numerical results, the researchers verified a higher energy absorption capacity for the REC structure in comparison to the conventional ones because a reduction in the maximum displacement of 28% was observed for the FEM simulations and the experimental tests. In addition, the absorbed impact energy increased by approximately 2%. Therefore, the REC model presents a relevant potential for applications requiring structures resistant against explosions.

The work by Lan et al. [223] proposes the development of AXSs for ballistic applications based on a sandwich panel having its core built from a chiral hybrid structure. The sandwich panel core was fabricated by the selective laser melting (SLM) technique. and AlSi10Mg aluminum alloy powder was used. The panels were built using a 5052 aluminum alloy, while the auxetic re-entrant cores were filled with a PU foam. The ballistic performance was based on the comparison of a model without the foam and the other one filled with it. The ballistic test was performed with a projectile created from aluminum foam, with an incident velocity between 206 and 296 m/s, and a mass ranging from 302 to 364 g. The impact moment was recorded by a high-velocity camera, illustrated in Figure 26. The ballistic tests results have shown that the sandwich panel filled with PU presented severe delamination on the foam after the impact. However, it prevented greater delamination for the panels. On the other hand, the panel without a filling has shown severe delamination on its surface. The indentation region for both specimens exhibited bending, although the specimen filled with PU disclosed less bending due to the energy absorption.

Haq et al. [224] proposed a comparison of the auxetic sandwich panels' dynamic behavior against an explosion. The researchers performed FEM simulations, adopting hexagonal cores based on conventional honeycomb and auxetic star structures composed of AA2024 aluminum alloy, while the panels were made of a material known as "Armor Steel". The explosion simulations were performed using trinitrotoluene (TNT), in concentrations of 1.5, 3 and 5 kg, and dropped over the sandwich panels on heights of 100, 300 and 500 mm. The FEM explosion simulations' results have shown that the auxetic cellular structures absorbed 28% more energy than the conventional honeycomb model. The auxetic cores applied on sandwich panels have demonstrated effectiveness in absorbing a huge amount of energy displaying a relatively smaller deformation for the back panel. The cellular wall structure provides an increase in the energy absorption capacity by the uniform dissipation of impact energy. For the load of 1.5 kg, the findings revealed that delamination did not occur on the structure; on the other hand, for loads of 3 and 5 kg, the simulation.





Yan et al. [225] manufactured sandwich panels with an auxetic core focusing on antiblast systems applications. The sandwich panel was fabricated from Q345 steel sheets, and the core based on a re-entrant structure was made of AlSi10Mg aluminum and constructed by the SLM method. An epoxy resin was applied to attach the core and the panels. The blasting test was performed using 500 g of TNT, placing it 10, 15 and 25 cm above the panel, as demonstrated in Figure 27a. A correlation was carried out with a structure manufactured by the same method. However, the core was a honeycomb non-auxetic model. The blasting test revealed that the auxetic core panel presented less deformation, as depicted in Figure 27b, attaining a maximum value of 19.58 mm, while the hexagonal core panel disclosed 26.29 mm after the explosion. This difference is associated with the amount of absorbed energy, where the AXS material displayed a higher absorption without fracturing. Figure 27c illustrates the panel after the explosion. It is possible to notice the damaged core, in which a re-entrant structure was completely disfigured near the explosion location, but the panel was not fractured. Moreover, the hexagonal core panel exhibited in Figure 27d presented a higher deformation since it absorbed less energy. In addition, the hexagonal core was fractured and bent out of shape while the explosion occurred, and delamination on the front panel has also been detected. These results unveil that the AXS is capable of absorbing greater amounts of energy, and, for this reason, it is suitable for anti-blast system applications.

Critchley et al. [226] investigated the cellular wall angulation effect upon the explosion resistance for re-entrants' AXSs. The samples were manufactured by the fused deposition modeling (FDM) method using a thermoplastic polyurethane (TPU). Five specimens were processed, with a range of cellular wall angulation and, as a result, the following structures were developed: 60° and 75° re-entrant, 90° square, and 105° and 120° hexagonal. Blasting tests were performed in a shocking tube, which simulates a controlled explosion on a lower scale and records the internal explosion reactions. The test findings have shown that the AXS cellular wall angulation is of utmost importance for the blast mitigation, where the 75° (re-entrant) angulation disclosed a mitigation of 23%, whereas the 60° model displayed a value of 12%. The hexagonal structures yielded a blast amplification effect, where the 105° and 120° angulation have shown values of 60% and 277%, respectively.



**Figure 27.** (a) Blasting test setup; (b) comparison of the core deformation; (c) damage mode of auxetic sandwich; (d) damage mode of honeycomb sandwich. Reprinted with permission from Ref. [225]. Copyright 2023, Elsevier.

Usta et al. [15] portrayed the high velocity impact behavior for curved sandwich panels. They were fabricated from CFRP sheets, and the distinct cores were based on no-auxetic PU foams manufactured by CNC, with auxetic PLA presenting a re-entrant structure produced by FDM. High velocity impact tests were performed on a single stage air gas machine that simulates a gun. A spherical steel projectile was used with a radius

and velocity of 5 mm and 100 m/s, respectively. The impact test results exposed an increase in the energy absorption as the curvate diminished for the panels and re-entrant cores. The sandwich panels having PU foams disclosed a superior impact resistance as a consequence of their synergistic interaction with the CFRP sheets. The failure mechanisms for the AXS and the PU foam are characterized by a fracture on the superior sheets, where the fibers rupture and matrix cracks have an influence. The foam cores are exposed to shear and crush deformation, while the auxetic core presents bends and cellular wall ruptures. Nevertheless, AXSs portrayed superior SEA values in comparison to the PU foam structures, suggesting that AXSs may have a relevant role in ballistic resistance. Meanwhile, other variables must be investigated in order to improve these metamaterials' resistance.

Wu et al. [64] investigated the AXSs impact resistance developed with Kevlar foils based on the Kirigami sheets, whilst the specimens were cut and rearranged on a 3D hexagonal and re-entrant design. Among the hollow spaces of the structure, shear stiffening gel (SSG) was introduced. The tests revealed that the AXS disclosed higher flexibility and resistance than the hexagonal model. The re-entrant model joined with the SSG filing developed and increased up to 76% in comparison to the hexagonal model also filled with the same material. This result is a consequence of the mechanical behavior provided by an NPR, but also the thickening behavior supplied by the SSG. This research does not make a ballistic application approach. However, the employment of SSG as a filling for AXS might provide great findings on absorption energy and ballistic resistance investigations [61,228]. Furthermore, the SSG is able to enhance its hardness when a shear load is increased because of its thickening that raises the mechanical resistance [229,230]. The same phenomenon is found for the shear thickening fluid (STF), which is extensively used on fabrics for ballistic demands [231–233].

## Brief Summary

A brief summary of this section is intended to reveal that, among the several sectors in Table 2, from aerospace to textile, AXS for military, high-velocity impact protection is included. However, only a few investigations [225,226] have used 3D-printed AXS, which is another open opportunity for future research works.

## 6. Conclusions

An impressive range of types and models of auxetic structures (AXSs), from the initially proposed re-entrant pattern to the novel cross-petal AXS structure for military applications requiring absorbing blast energy, are presently being investigated and industrially developed.

The numerous proposed AXS structures, independent of their complex shapes, can now be more cost-effectively fabricated by several techniques, either by traditional techniques or by AM, also known as 3D printing. In addition to being cheaper, 3D-printed AXS structures have the advantage of fast and easy fabrication.

Looking ahead, there is significant potential for the continued growth and development of 3D-printed AXS structures for use in high-velocity impact applications. As such, we can expect to see continued research and product development in this area in the coming years.

### 7. Final Remarks

Sandwich panels, particularly those with honeycomb structure inner core, have received considerable attention in the past few decades with an exponential growth in research works. Applications of these honeycomb panels extend to diversified industrial sectors, including military owing to their higher energy absorption. In particular, AXSs honeycomb patterns fabricated by AM have recently been the subject of relevant investigation on their ballistic characteristics, as in the remarkable work of Yan et al. [11] and a prominent review paper on anti-blast performance by Bohara et al. [21]. In the present review, the main points of published AXS/3D-printed articles discussing high-velocity impact were critically discussed. All of these reviewed articles emphatically indicated the superior resistance of AXS/3D-printed sandwich panels to shockwave blast and ballistic impact. One condition, however, is still uncertain in the opinion of Bohara et al. [21]. Under very high impact loads, the blast shockwave propagates much faster than the stress wave. As a result, the AXSs might not have time to deform with an NPR. The authors also recommended further research on improvements in 3D printing technology to produce large-scale AXSs to be applied in armors for high-velocity impact protection. The combination of AM and discrete assembly methods is suggested as a solution for today's size limitation of 3D printers, in order to improve, optimize and fabricate AXS-based ballistic armor. As for the specific case of honeycomb AXS, constructed by SLM/AM, Yan et al. [11] concluded that carbon fiber reinforced polymer, as an outer sheet, is a potential reinforcement for associated sandwich panels with excellent ballistic performance.

Although the commercial use of AXS/AM-based high-velocity impact protective armor is still in its infancy [21], all presently reviewed works strongly support indisputable future military interest.

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#### Abbreviations

The following abbreviations are used in this manuscript:

- v Poisson's Ratio
- $\lambda$  Wavelength
- ABS Acrylonitrile Butadiene Styrene
- ACC Auxetic Contacted Cube
- Ag Silver
- AM Additive Manufacturing
- Au Gold
- AXS Auxetic Structures
- BCP Block Copolymers
- BCPS Braced Cross-Petal Structure
- CFRP Carbon Fiber Reinforced Polymer
- CM Conventional Material
- CNC Computer Numeric Control
- Cu Copper
- CPS Cross-Petal Structure
- CVD Chemical Vapor Deposition
- DLW Direct Laser Writing
- E Young's Modulus
- FDM Fused Deposition Modeling

FEM

Fe<sub>3</sub>O<sub>4</sub>

Finite Elements Method

Magnetite

G	Shear Modulus
G <sub>IC</sub>	Fracture Initiation Toughness
GNP	Graphene Nanoplatelets
GPa	Gigapascal
Н	Hardness
HGS	Hourglass Structure
Κ	Bulk Modulus
K <sub>IC</sub> *	Fracture Toughness
LDPE	Low Density Polyethylene
LRP	Laser Rapid Prototyping
MPP	Multi-Photon Polymerization
NIJ	National Institute of Justice
NiTi	Nickel Titanium
NPR	Negative Poisson's Ratio
PDA	Polydiacetylene
PLA	Polylactic Acid
PP	Polypropylene
PU	Polyurethane
RAH	Re-entrant Arrowhead Structure
RCA	Re-entrant Chiral Auxetic
REC	Re-entrant Circular
SAH	Star Arrowhead Structure
SEA	Specific Energy Absorbed
SEBM	Selective ELectron Beam Melting
SLA	Microstereolithography
SLM	Selective Melting Laser
SLS	Selective Laser Sintering
SMEP	Shape Memory Epoxy Polymer
SMP	Shape Memory Polymers
SPPW	Self-propagationg Photopolymer Waveguides
SSG	Shear Stiffening Gel
STF	Shear Thickening Fluid
TNT	Trinitrotoluene
TPU	Thermoplastic Polyurethane
UV	Ultraviolet
VPP	Vat Photopolymerization
$ZrO_2$	Zirconium Oxide

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